



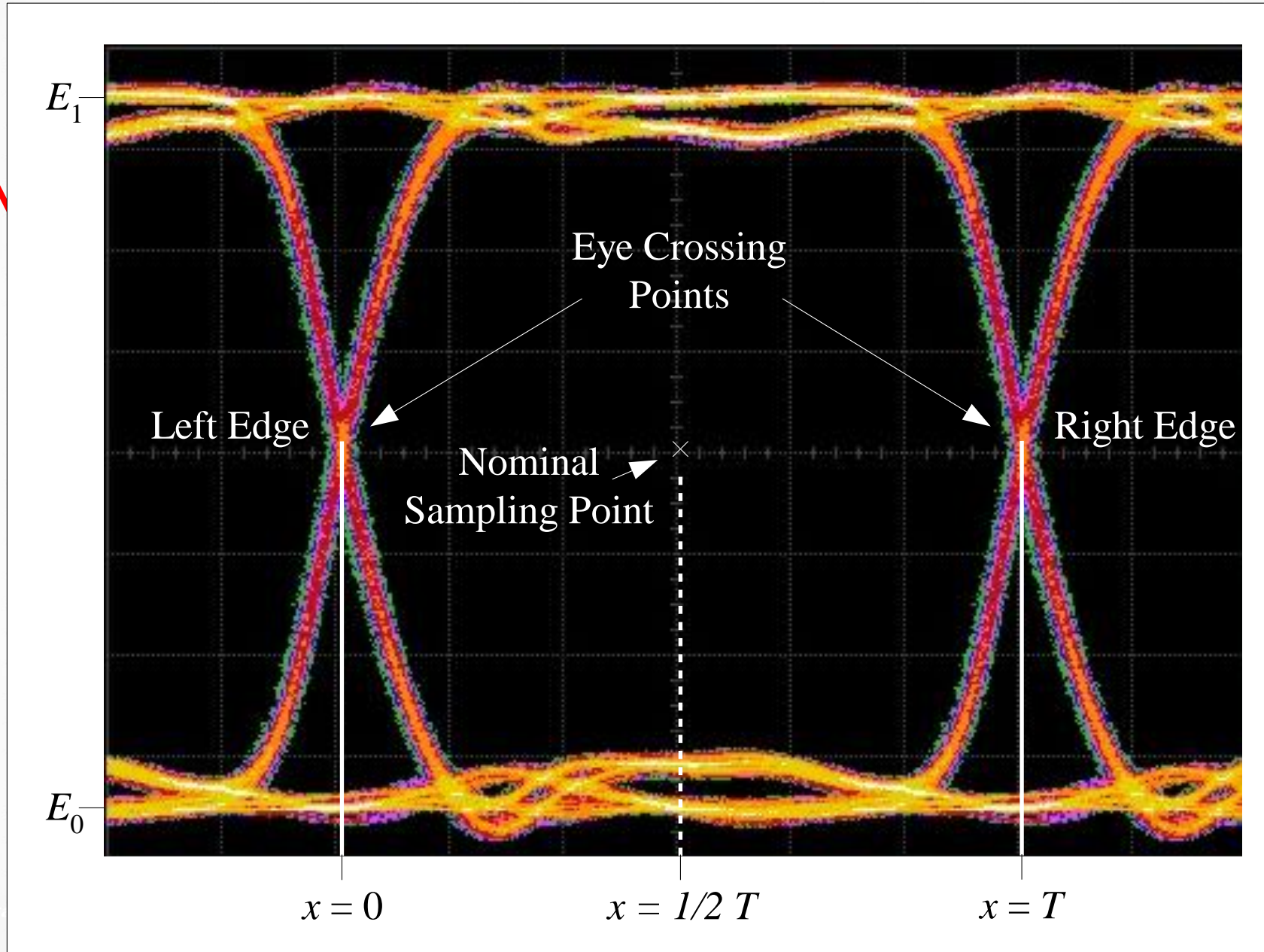
**ENGINEERS**  
NEVER STOP LEARNING

# Advanced Jitter and Eye-Diagram Analysis

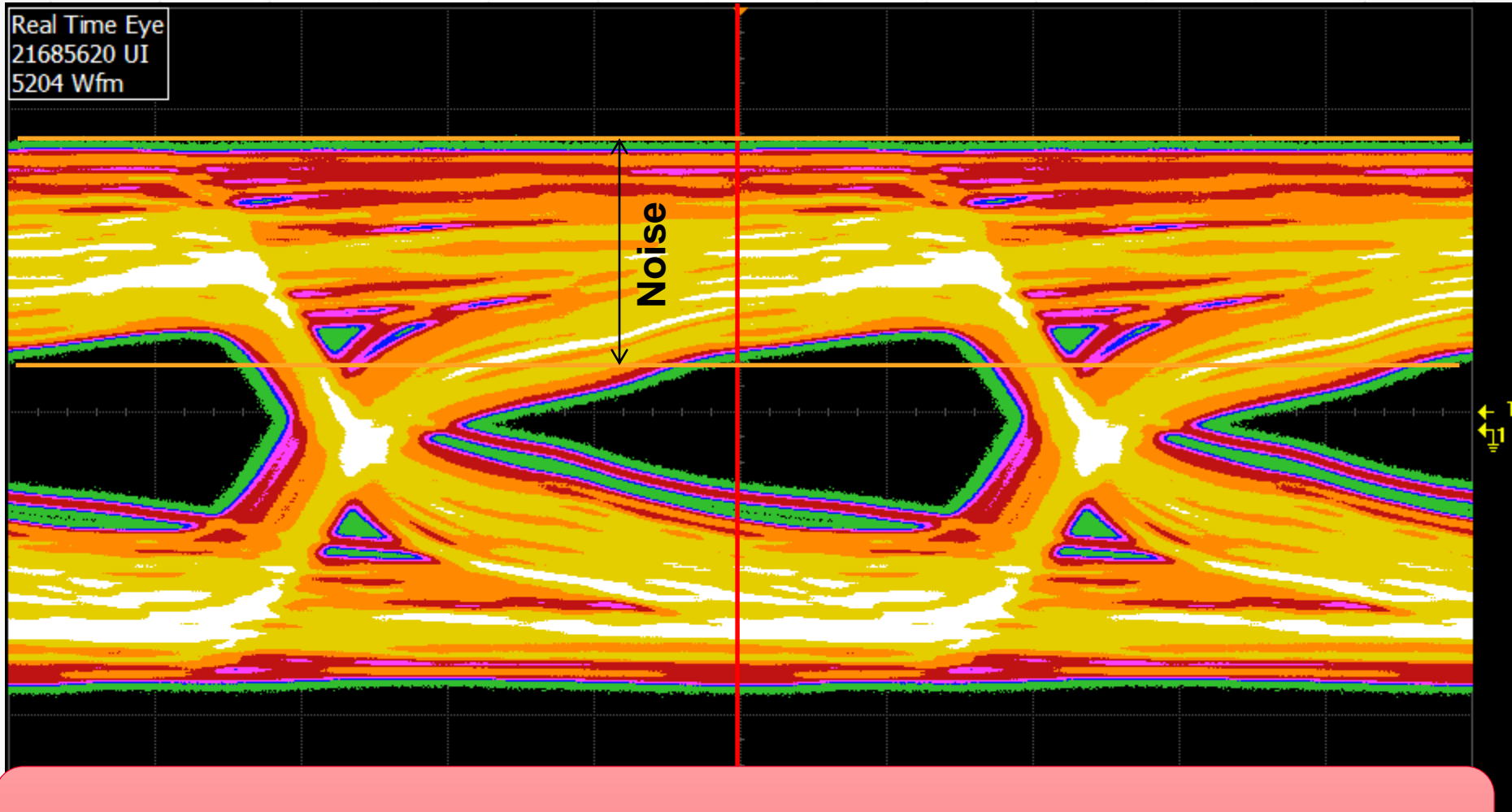
*Project Manager / Keysight Taiwan AEO*

*余宥浚 Jacky Yu*

# Constructing the Real-Time Eye

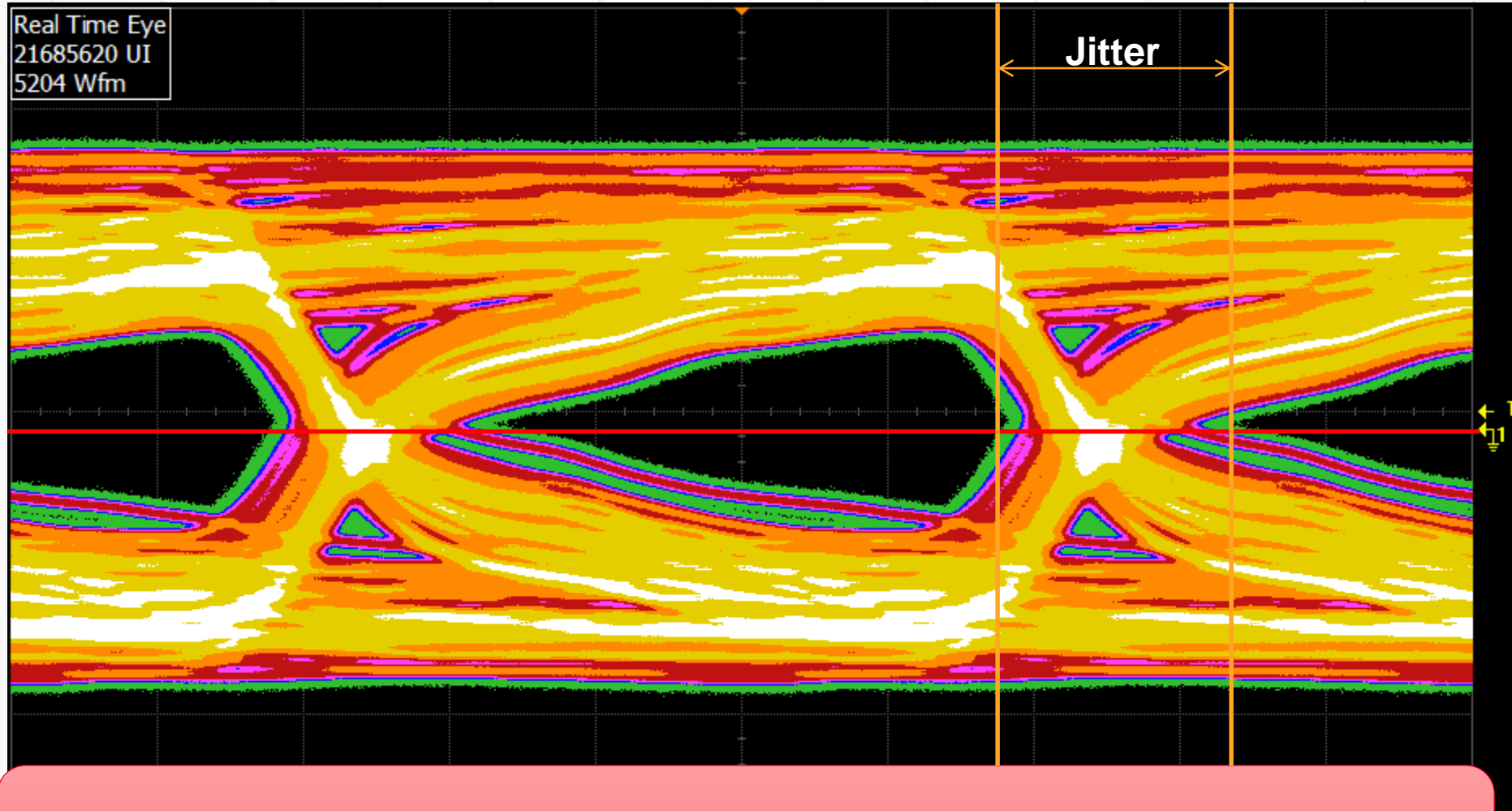


# Non-ideal Real-Time Eye



What happened to our eye opening?

# Non-ideal Real-Time Eye



What happened to our eye opening?

# Pause for definitions

**A dictionary definition of the verb “jitter”:**

*To make small, quick, jumpy movements.*

**In the digital design world, jitter is defined as:**

*The deviation of the significant instances of a signal from their ideal locations in time.*

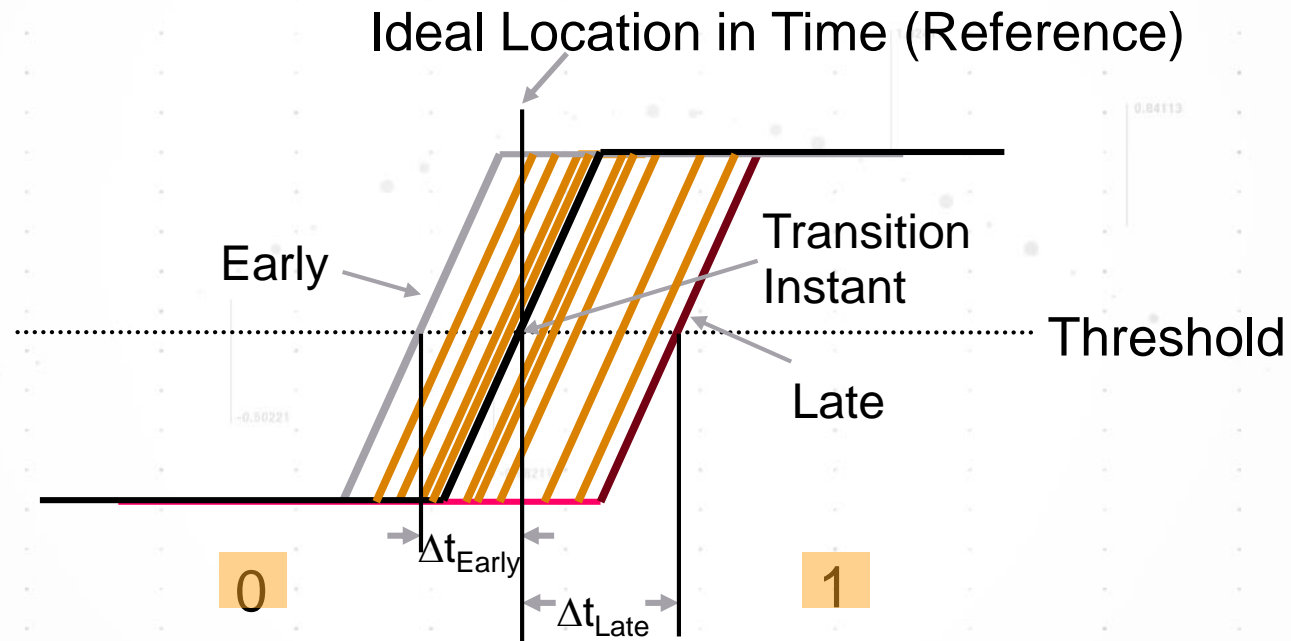
**The significant instances for data signals are the transitions (edges)**

**The ideal locations for the transitions are determined by the time reference (clock)**

# Single Transition Jitter

We can see from the eye diagram, jitter effects the transitions of the data stream.

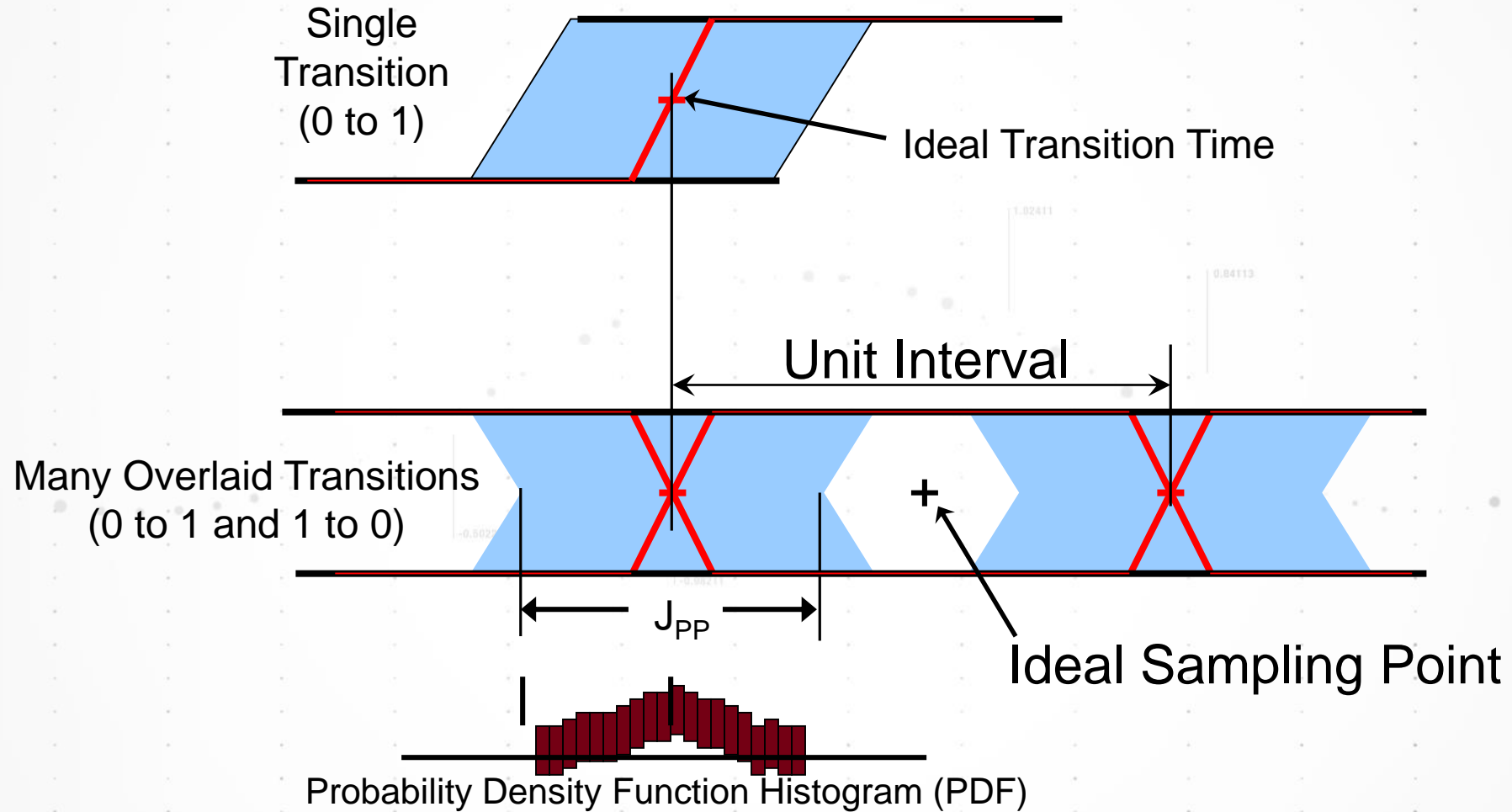
Let's take a closer look at a single transition.



$$\text{Peak-to-peak jitter} = J_{\text{PP}} = \Delta t_{\text{Early Pk}} + \Delta t_{\text{Late Pk}}$$



# Jitter and the Real-Time Eye



# It's all about Bit Error Ratio

- Noise and Jitter cause data transmission errors in digital systems
- These errors are characterized by the Bit Error Ratio (BER) of a serial data link
- BER is the primary measure of the *fidelity* of a link

$$\text{BER} = \# \text{ Transmission Errors} / \text{Total} \# \text{ Transitions}$$

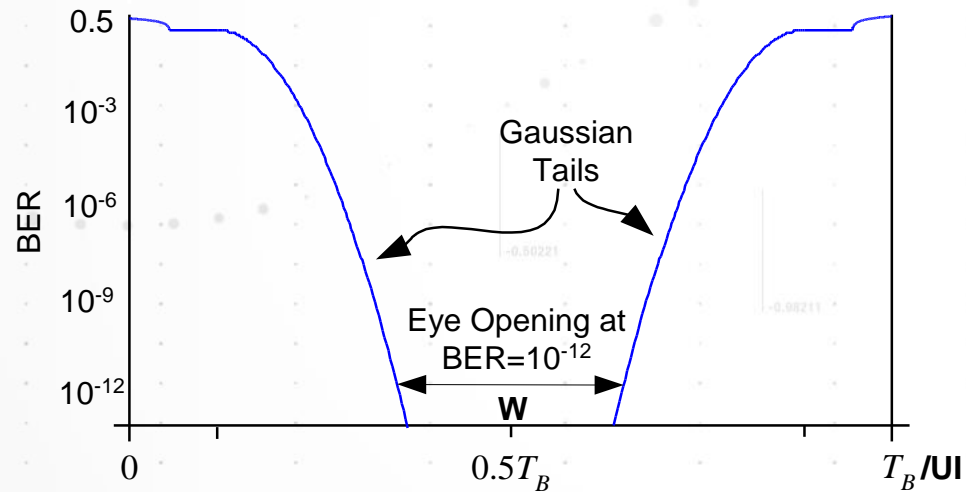
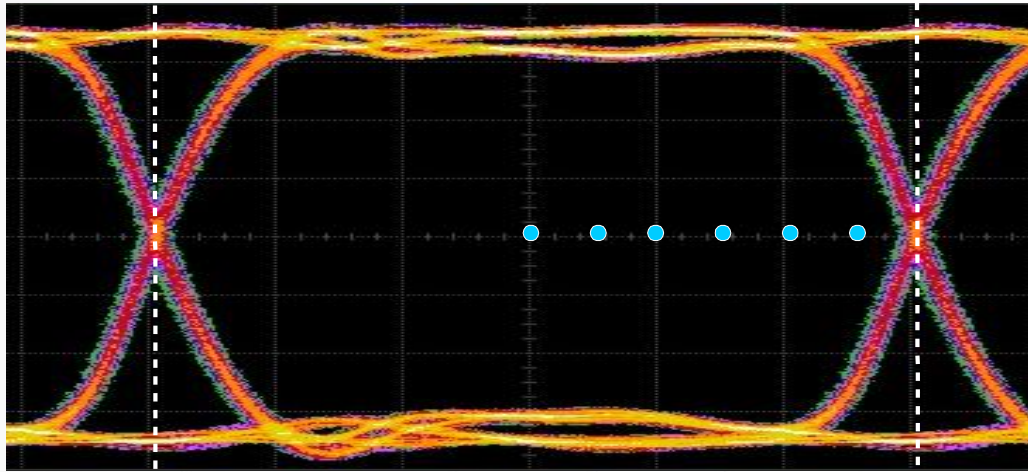
When data rates were low, designers were mainly concerned with functionality (1s and 0s)

With rates > 1 Gbps, the analog nature of signals becomes significant

*Noise and jitter* affect system BER and the quality of a data link



# Measuring Jitter: Bit Error Ratio (BER) Testing



Requires specialized equipment  
and very slow

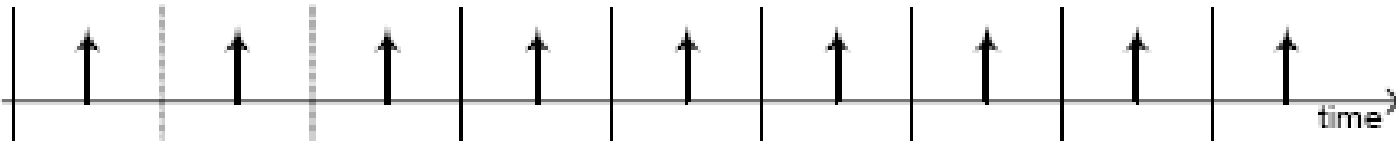
- ❖ The only way to *directly* measure Total Jitter is with a Bit Error Ratio (BER) test.
- ❖ Sample at various points along unit interval, directly measure BER at each point. Plot “bathtub” curve.

$$TJ(BER) = UI - W$$

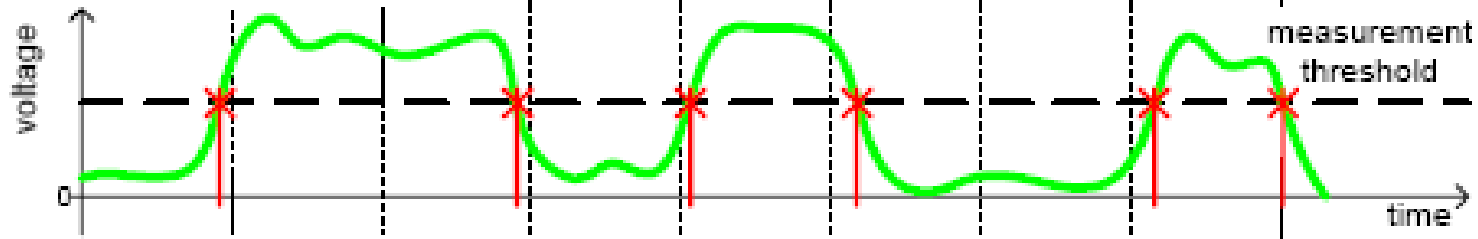
# Advanced Jitter Analysis with Real-time Oscilloscopes

## JITTER AND TIME INTERVAL ERROR (TIE)

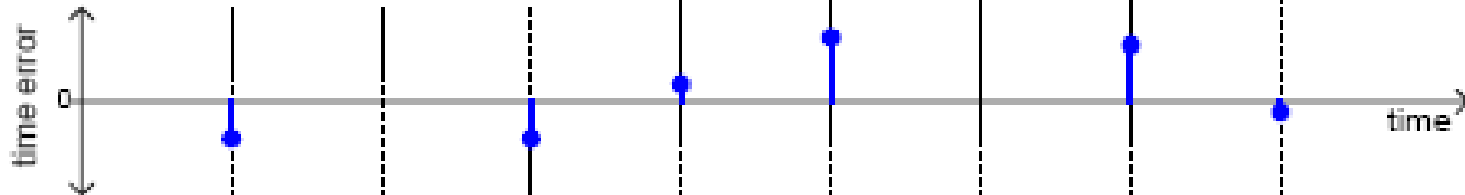
(a) Clock Reference



(b) Source Waveform



(c) Time Interval Error (TIE)



On an oscilloscope we monitor the waveform transitions and note the jitter at each transition point. This is called the Time Interval Error (TIE) record.

Measures total jitter of the *acquisition*. The more transitions you measure, the greater TIE will become.

Waveform transitions deviate from expected transition time

Generate Time Interval Error (TIE) by measuring transitions versus reference clock

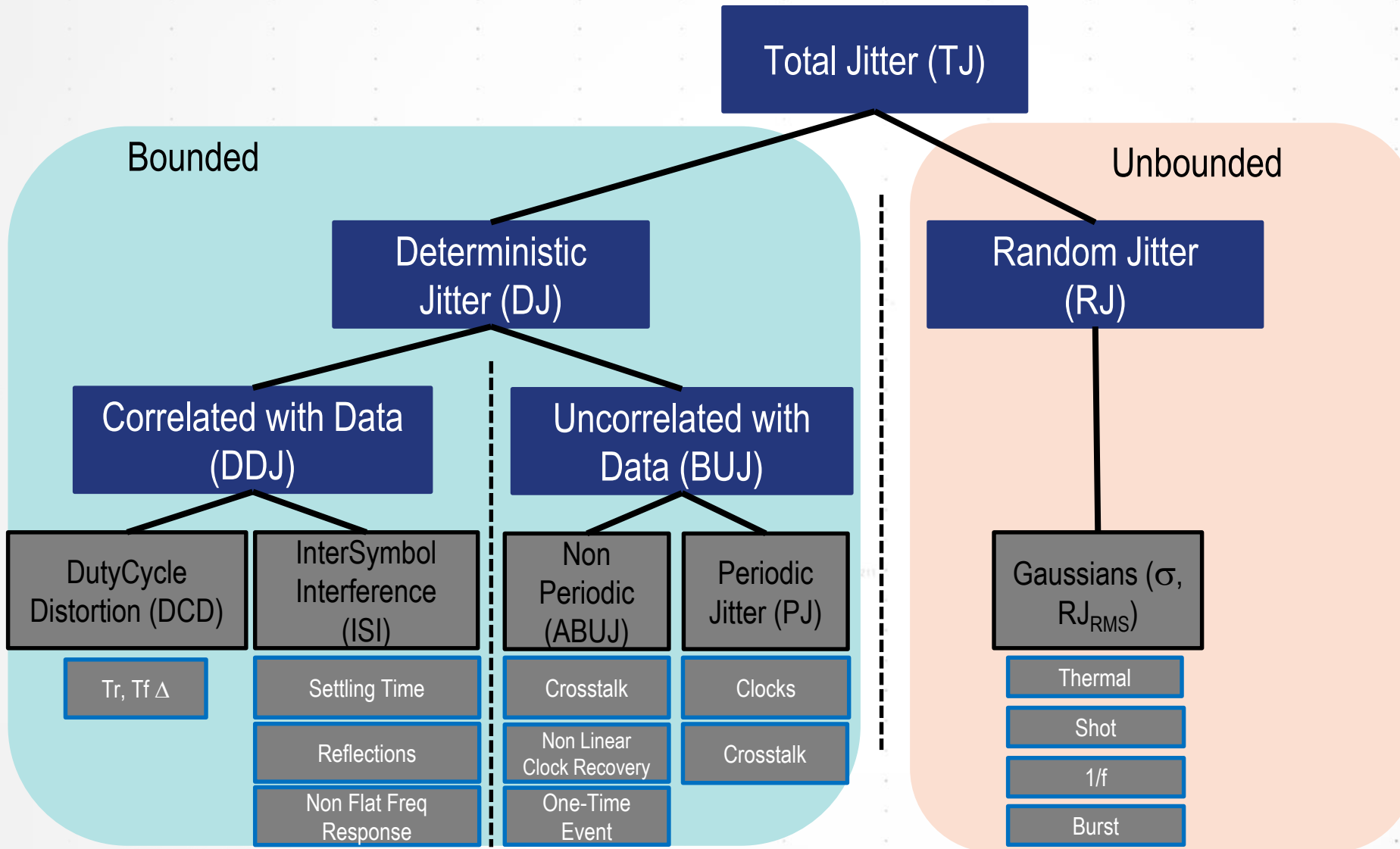
# Engineers Never Stop Learning

## ADVANCED JITTER ANALYSIS WITH REAL-TIME OSCILLOSCOPES

### Agenda

- **Review of Jitter Decomposition**
- Assumptions and Limitations
- Spectral versus Fail Fit Method
- Advanced Jitter Analysis with Crosstalk Removal Tool
- Scope Random Jitter Removal from Jitter Analysis
- Other Tools to consider for Jitter Analysis
- Summary

# Jitter Components

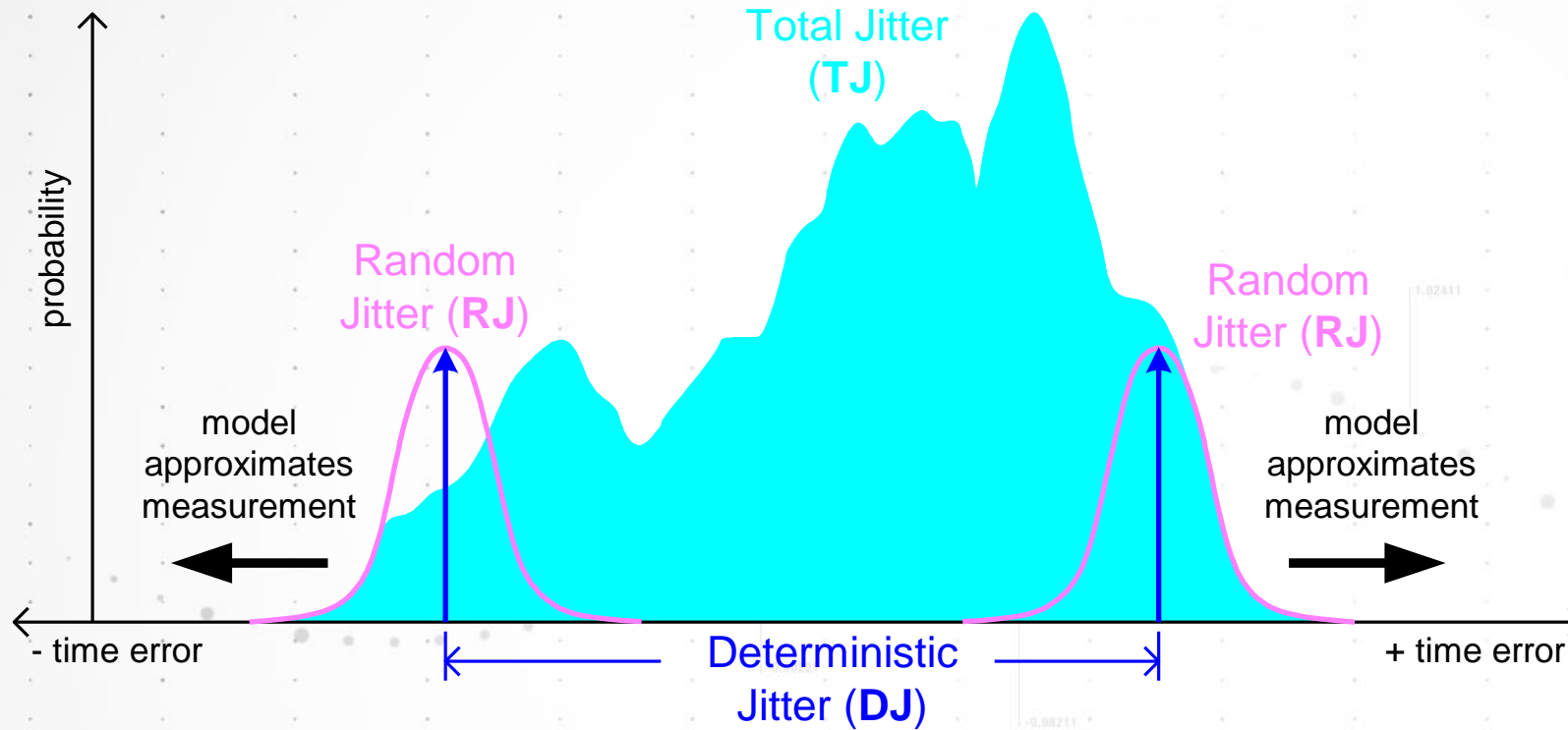


## Acronyms

- DDJ : Data Dependent Jitter
- BUJ : Bounded Uncorrelated Jitter

ABUJ : Aperiodic Bounded Uncorrected Jitter

# Dual Dirac Model



## Key Assumptions

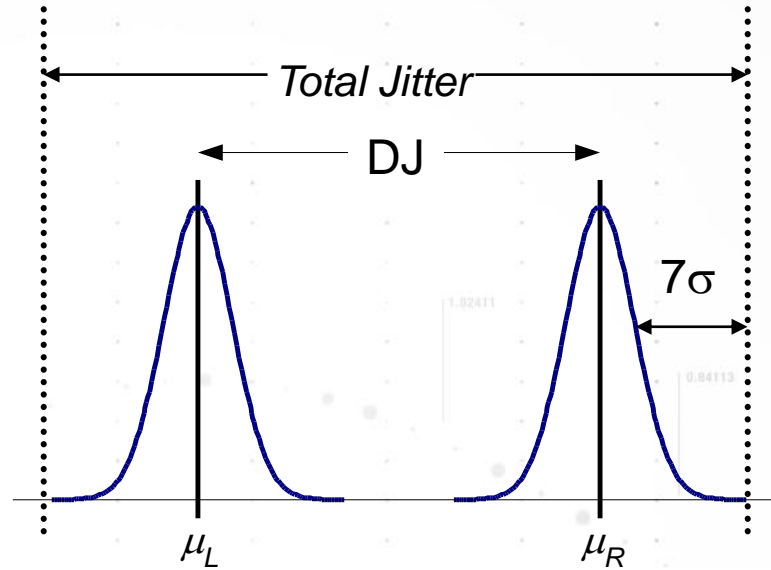
- Total Jitter at a BER can be predicted by a simple model using 'Deterministic' and 'Random' components.
- Gaussian distribution of random noise
- Stationarity of jitter distribution

# Dual Dirac Model – Total Jitter

BER	n
$1 \times 10^{-8}$	5.73
$1 \times 10^{-10}$	6.47
$1 \times 10^{-12}$	7.13
$1 \times 10^{-14}$	7.74

$$n = \frac{RJ_{pp} / 2}{\sigma}$$

(  $\sigma = RJ_{rms}$  )



$$TJ(BER) = UI - W$$

TJ can be measured directly using a BER test

OR

TJ can be calculated using RJ and DJ in the Dual Dirac model

$$TJ(BER) = 2n * RJ_{rms} + DJ$$

# EZJIT Jitter Analysis Suite

*For Infiniium Real-Time Oscilloscopes*

Jitter Trend, Histogram,  
and Timing  
Measurements

Advanced Jitter  
Decomposition:  
RJ/PJ/DDJ/DCD/ISI/ABUJ

Vertical Noise  
Analysis and  
Decomposition

EZJIT



EZJIT Plus



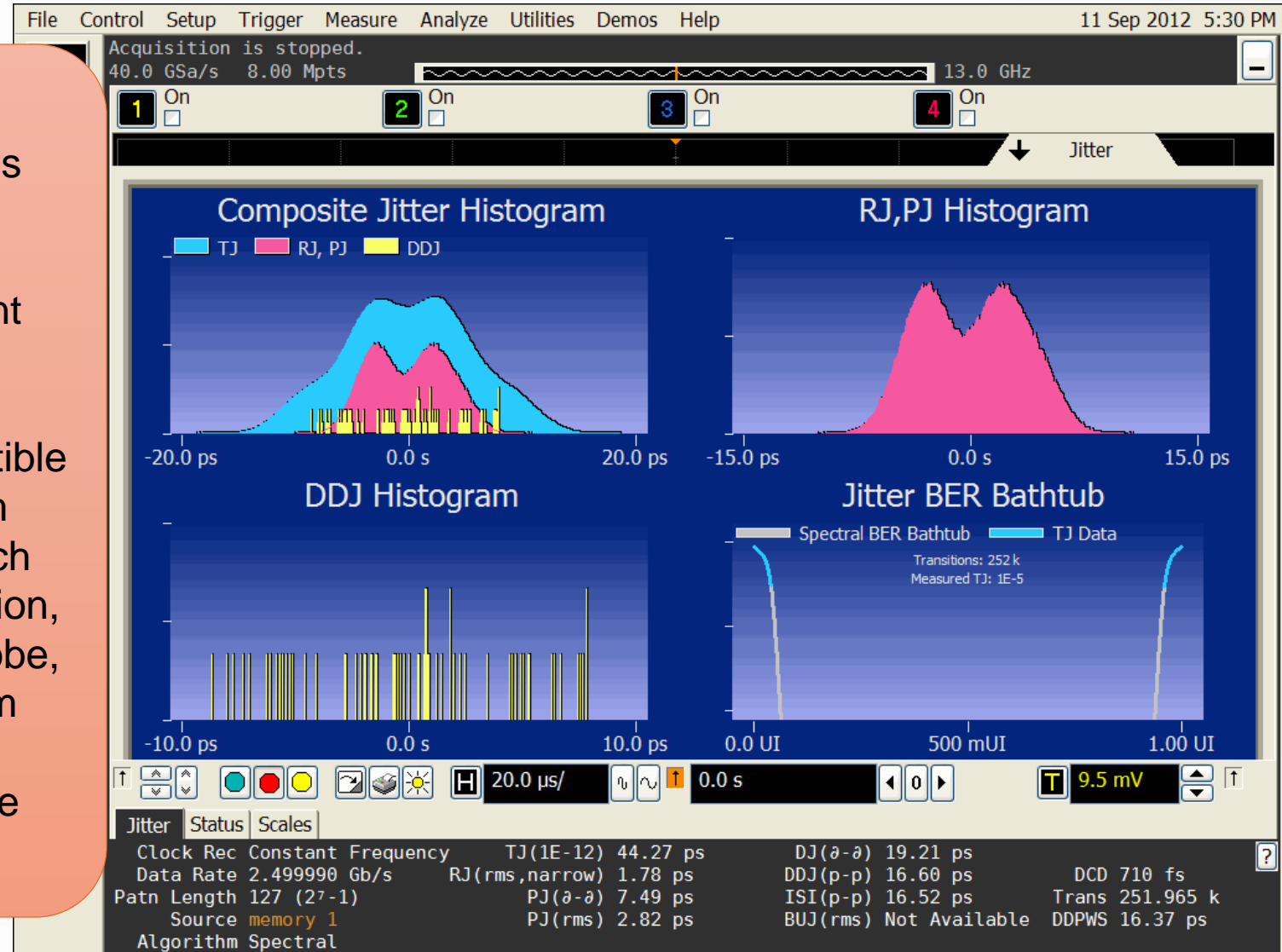
EZJIT Complete





# EZJIT Plus – Advanced Jitter Decomposition

- Easy to use wizard guides you through jitter measurement setup
- Fully compatible with Infiniium Software such as Equalization, PrecisionProbe, and InfiniiSim
- Customizable jitter views



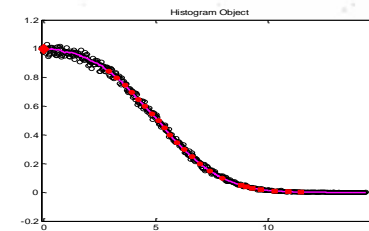
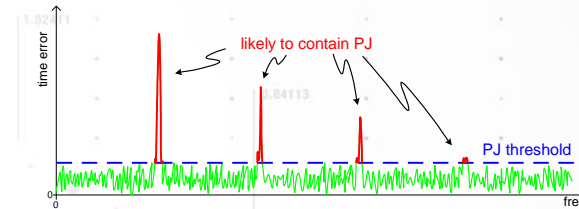
# Agenda

- Review of Jitter Decomposition
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- Spectral vs. Tail Fit Method
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# Spectral vs. Tail Fit Jitter Decomposition

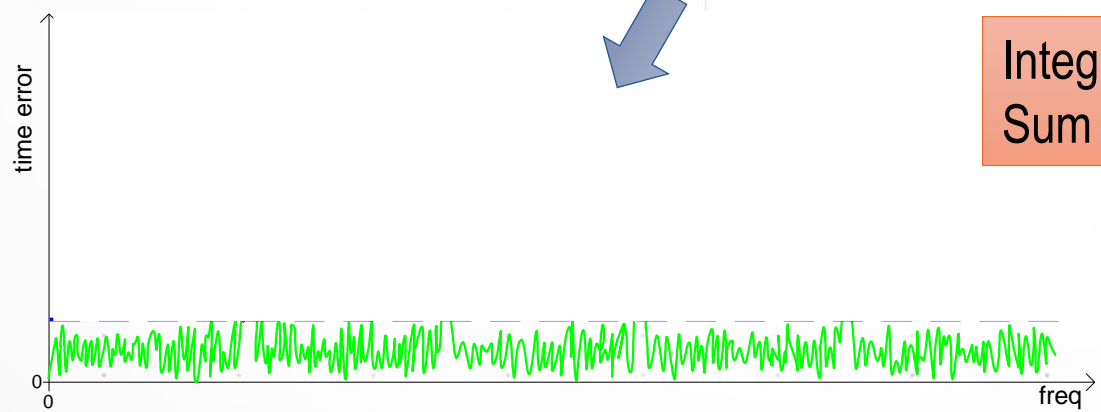
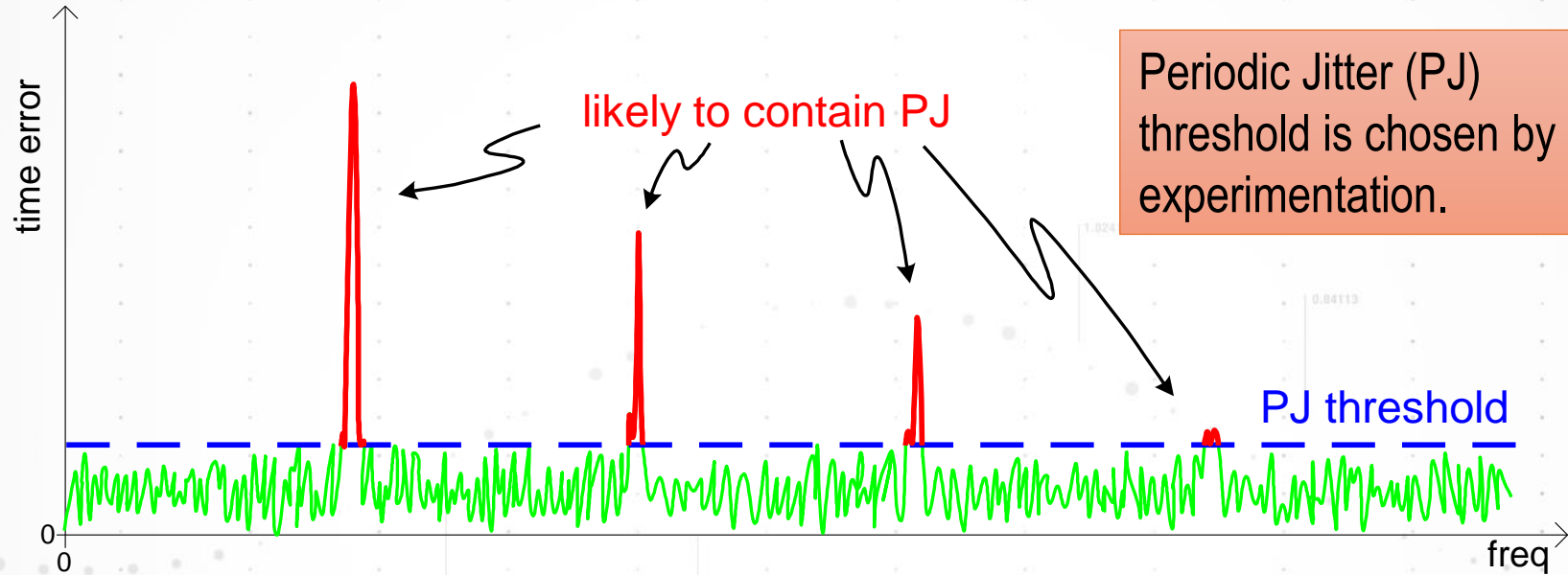
Random Jitter (RJ) Extraction Methods

RJ Extraction Methods	Rationale
Spectral	<ul style="list-style-type: none"><li>• Speed/Consistency to Past Measurements</li><li>• Accuracy in low Crosstalk or Aperiodic Bounded Uncorrelated Jitter (ABUJ) conditions</li></ul>
Tail Fit	<ul style="list-style-type: none"><li>• General Purpose</li><li>• Accuracy in high Crosstalk or ABUJ conditions</li></ul>



# Spectral Method – PJ Threshold

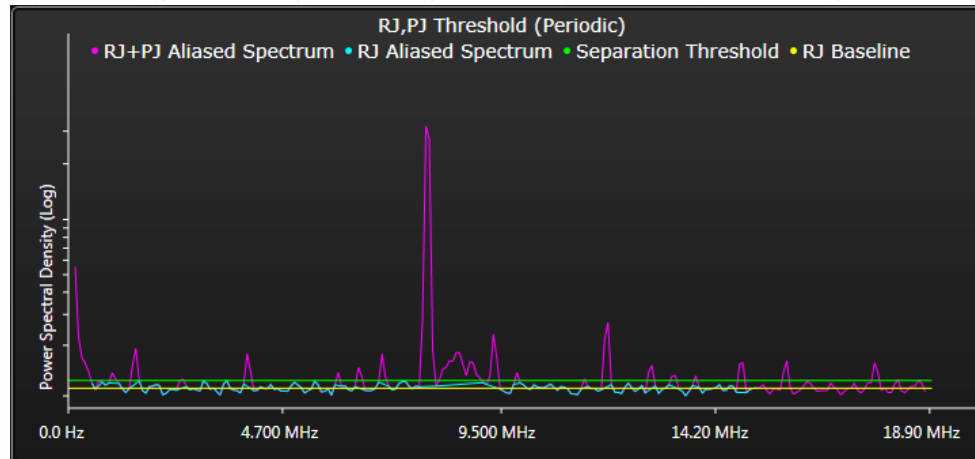
## Measurement Details



Integrate PSD to derive  $RJ_{RMS}$   
Sum the PJ components for  $PJ_{RMS}$

# Spectral Method – PJ Threshold

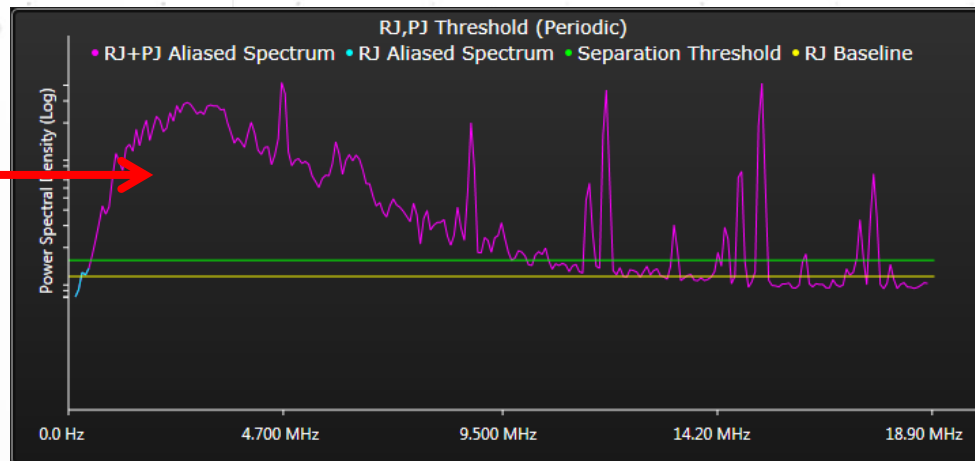
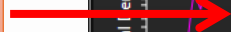
Handling of Different RJ, PJ Spectral Content



Separation occurs as described...

0.84113

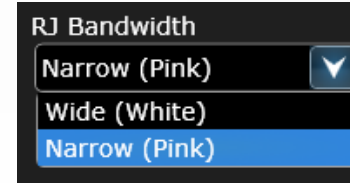
Is it RJ or PJ?



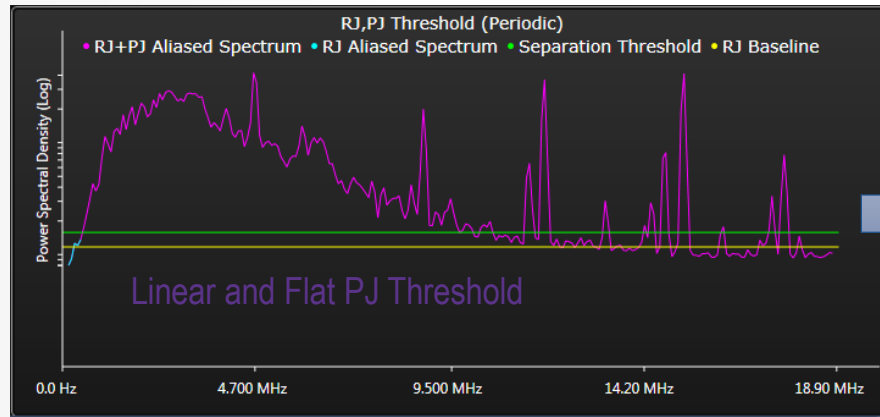
What do you do in this case?

# Spectral Method – PJ Threshold

Non-linear Period Jitter (PJ) threshold can help

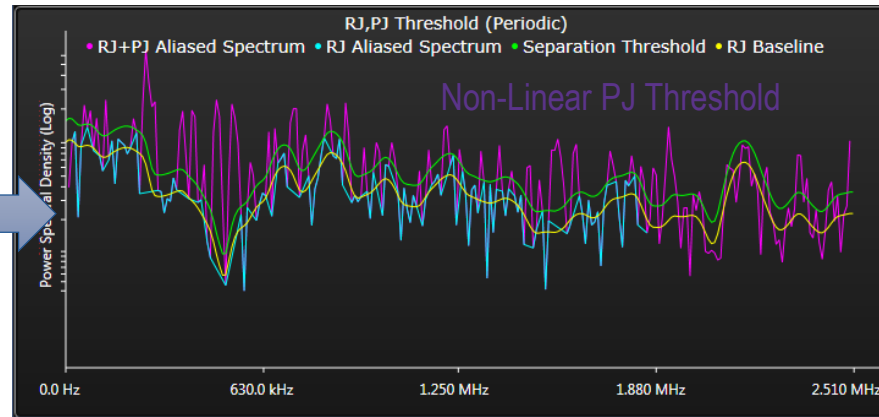


### Wide RJ Bandwidth Analysis



$$RJ_{RMS} = 1.06ps$$
$$PJ_{DD} = 93.17ps$$

### Narrow RJ Bandwidth Analysis

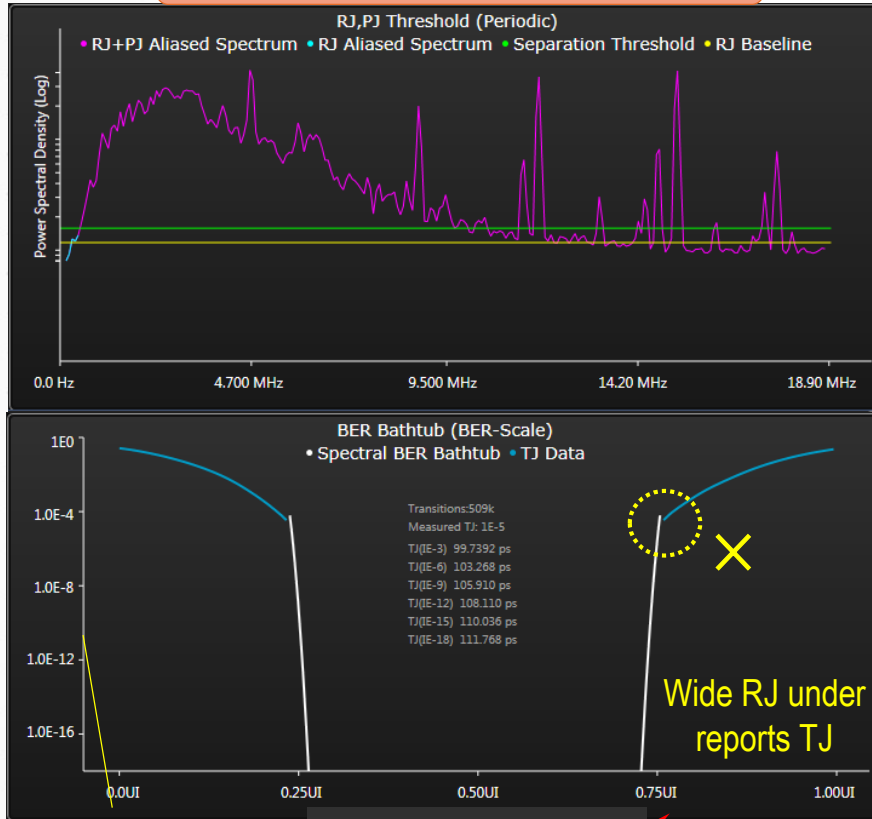


$$RJ_{RMS} = 9.66ps$$
$$PJ_{DD} = 27.18ps$$

Which PJ Threshold or RJ bandwidth analysis do you choose?

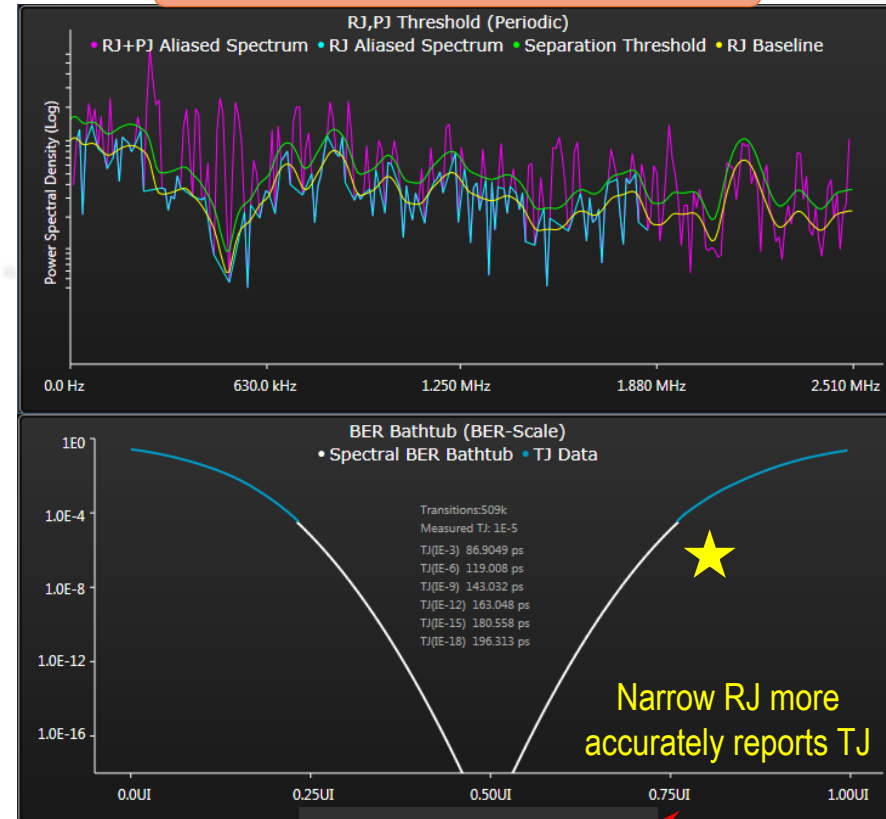
# Spectral Method – Wide vs. Narrow

## Wide RJ Bandwidth



TJ(1E-12)	108.11 ps
RJrms,wide	1.06 ps
DJ88	93.17 ps

## Narrow RJ Bandwidth



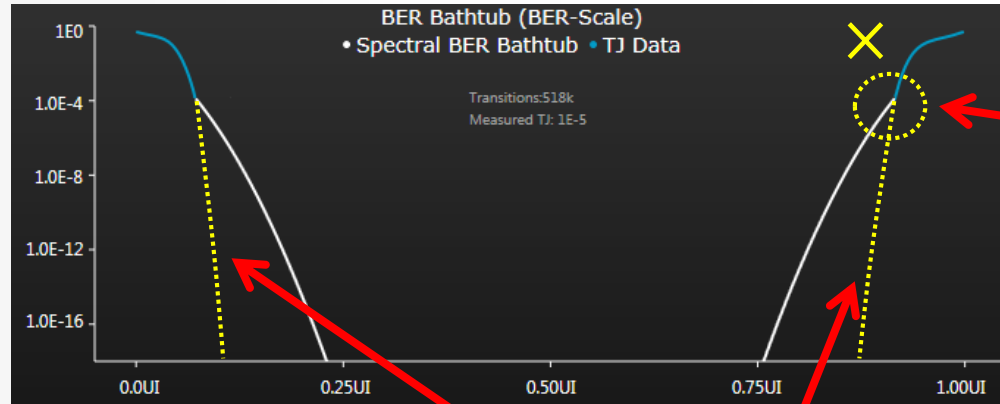
TJ(1E-12)	163.05 ps
RJrms,narrow	9.66 ps
DJ88	27.18 ps

*Smoothness of slope continuity between measured and extrapolated result on the bathtub plot indicates the better PJ threshold (RJ bandwidth) method.*



# Spectral Method with Presence of Crosstalk or ABUJ

(ABUJ = Aperiodic Bounded Uncorrelated Jitter)



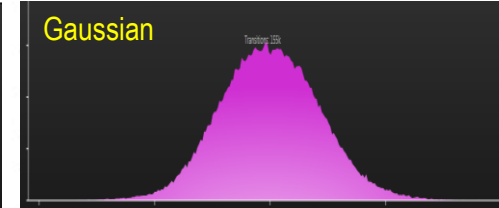
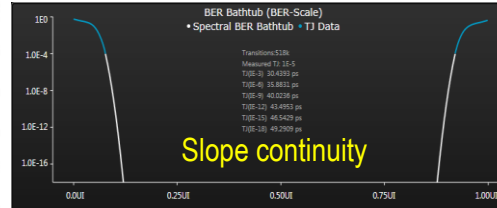
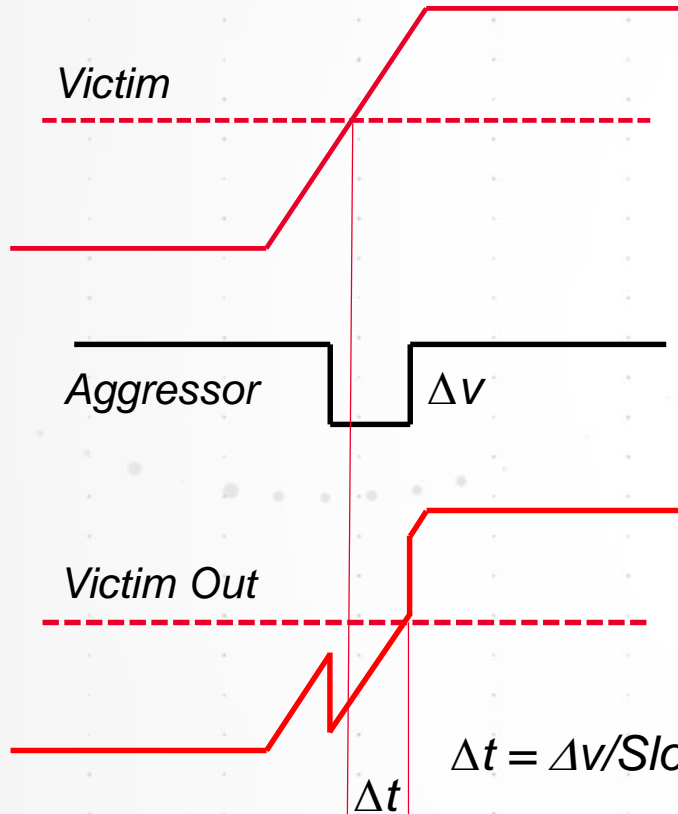
Something is wrong here...

Using the slope continuity concept we expect the extrapolated curve to look like this.

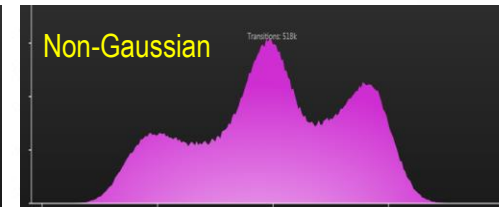
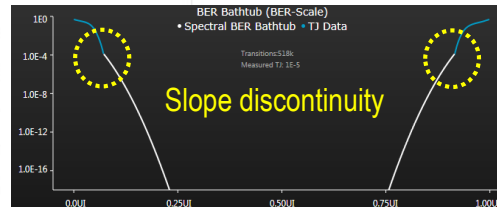
The RJ/PJ spectral extraction does not deal with Crosstalk or ABUJ well. The RJ is overestimated severely.

# ABUJ: Crosstalk or Ground Bounce

Amplitude interference uncorrelated with data and not periodic in nature.



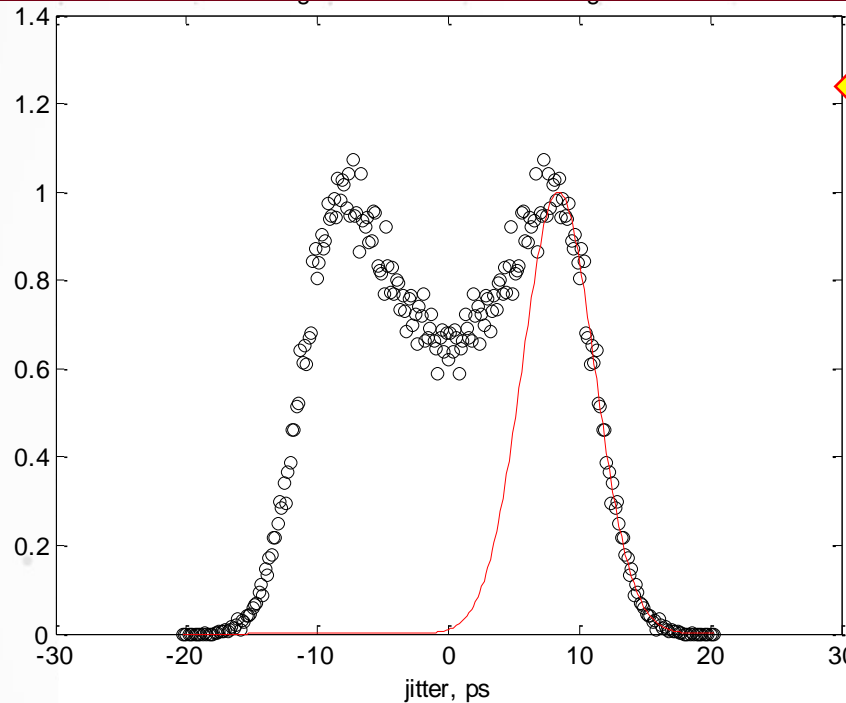
No crosstalk  
Bathtub and RJ,PJ Histogram



With crosstalk  
Bathtub and RJ,PJ Histogram

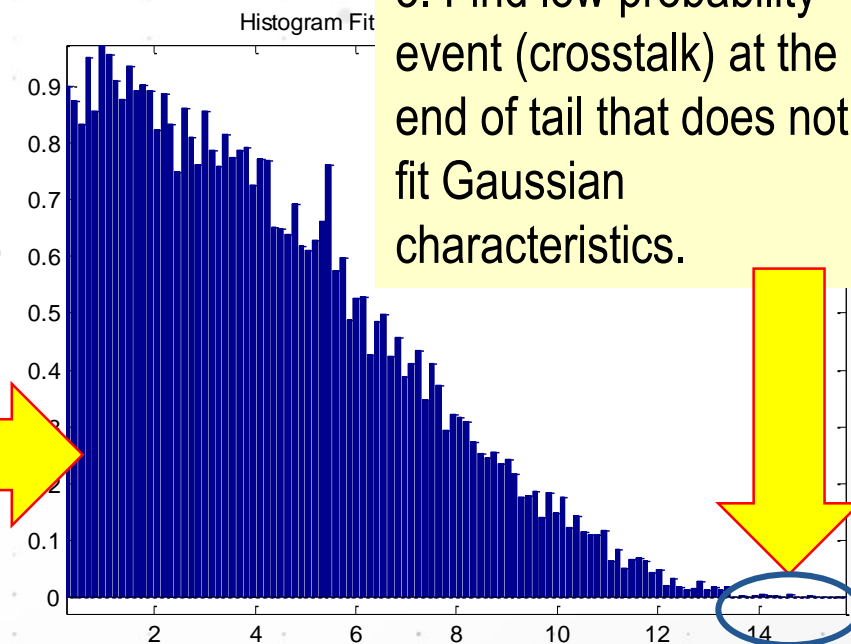
# Tail Fit Method – Gaussian Extraction

## MEASUREMENT DETAIL



1. Fit a Gaussian characteristic to the right and left extremes of the RJ/PJ histogram distribution.

2. Actual data is never smooth

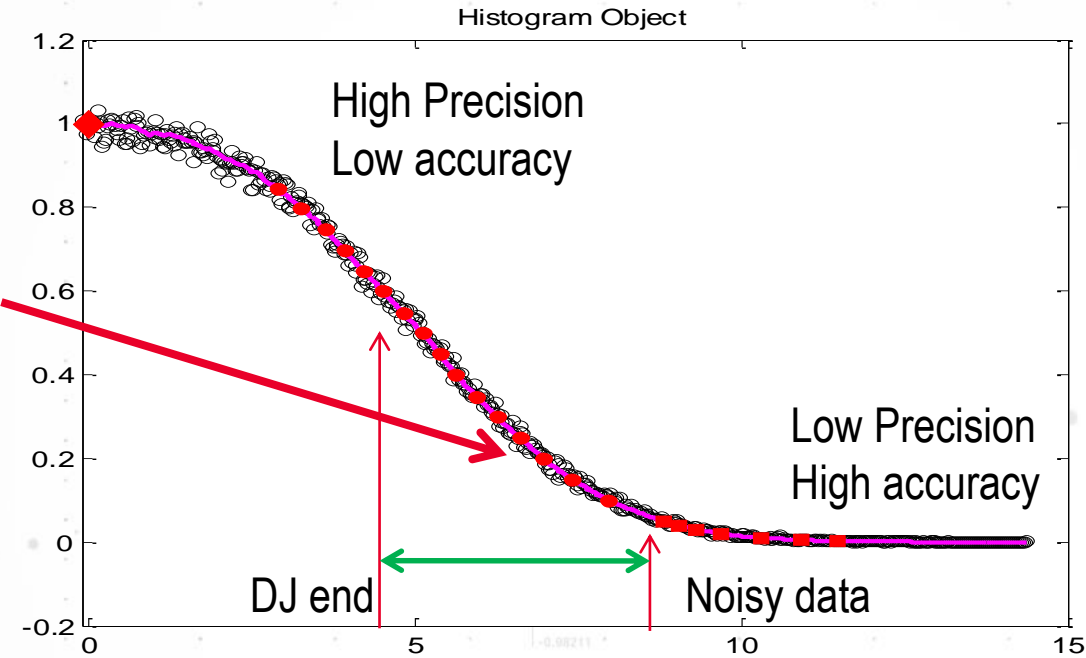


3. Find low probability event (crosstalk) at the end of tail that does not fit Gaussian characteristics.

# What Makes Tail Fit Hard

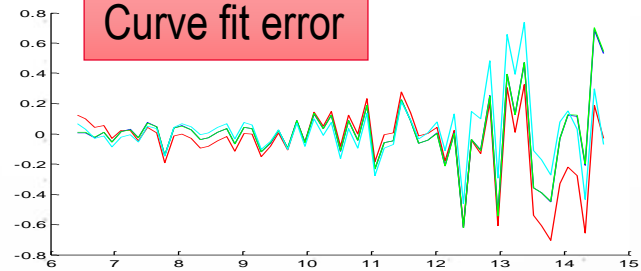
Measurement Detail

Fit Window



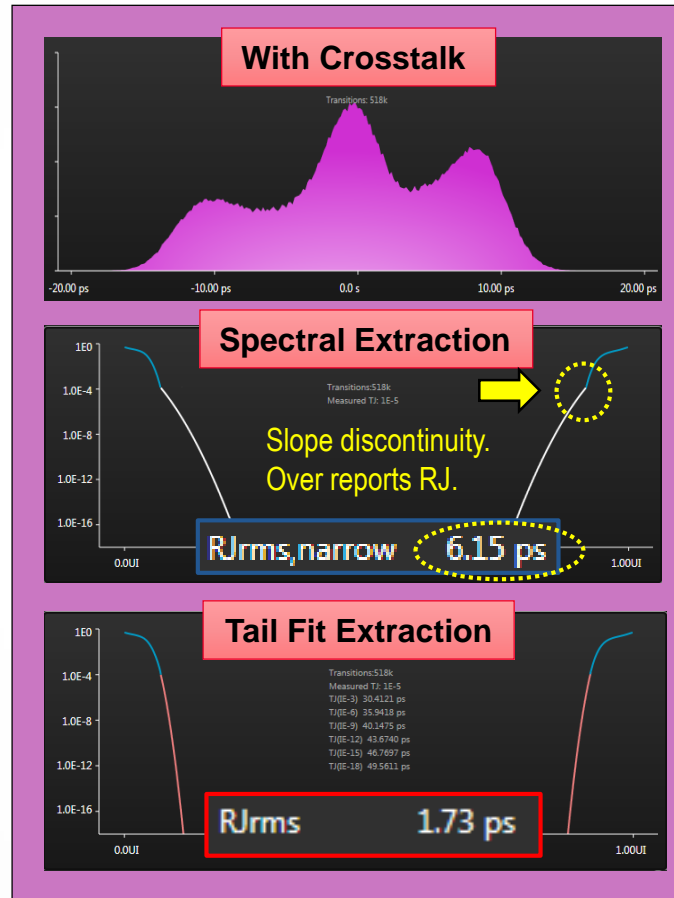
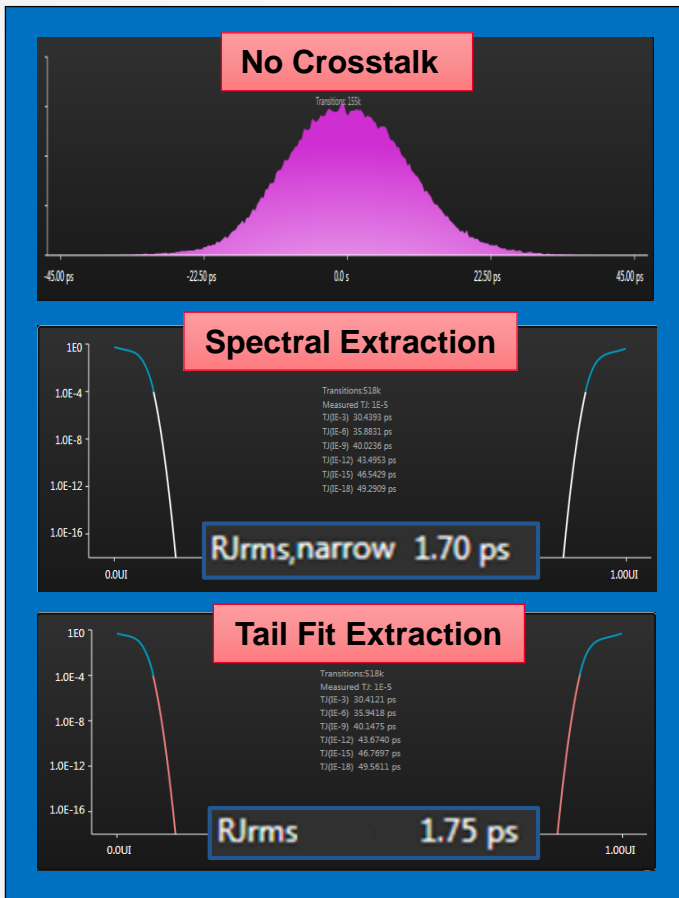
Hard to detect Crosstalk events out in the tail. Might take longer time for Tail Fit results to converge.

Curve fit error



# RJ Extraction with Presence of Crosstalk (ABUJ)

## SPECTRAL VS. TAIL FIT EXTRACTION



Analyze the bathtub plot with both RJ extraction modes to explore the presence of crosstalk or ground bounce.

# Agenda

- Review of Jitter Decomposition
- Assumptions and Limitations
- Spectral vs. Tail Fit Method
- **Advanced Jitter Analysis with Crosstalk Removal Tool**
- Scope Random Jitter Removal from Jitter Analysis
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# Jitter Analysis with Crosstalk Removal Tool

## Crosstalk Identification

- Which signals are coupling onto your victim?

## Crosstalk Quantification

- How much error and jitter do each aggressor add to your victim?

## Crosstalk Removal for Jitter Analysis

- What would your signal look without crosstalk present on victim?
- How much jitter margin can be recovered without crosstalk?
- If the signal was failing the jitter spec, can it pass without crosstalk?

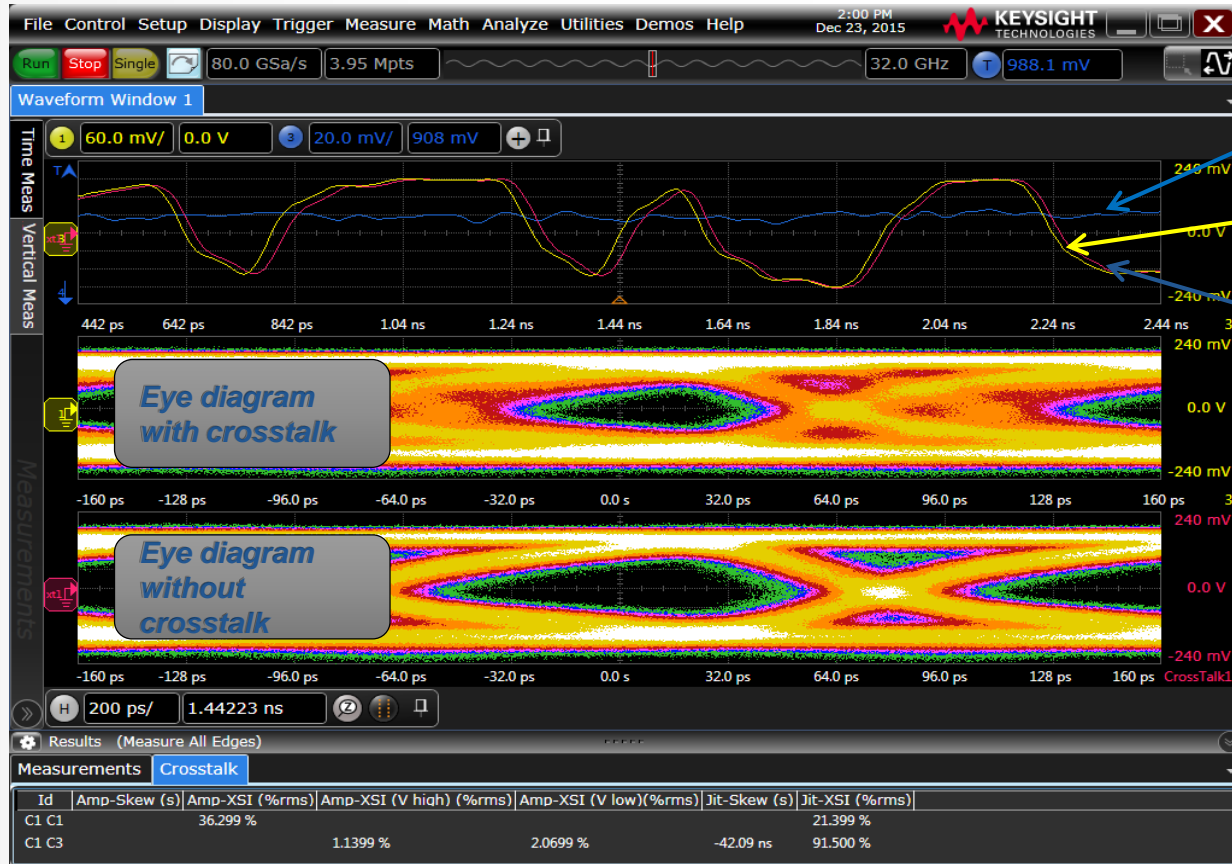


### *Assist in making important design decisions:*

- *Is it worth reducing crosstalk impact in design?*
- *Where to improve?*



# Remove Crosstalk from Victim Signal



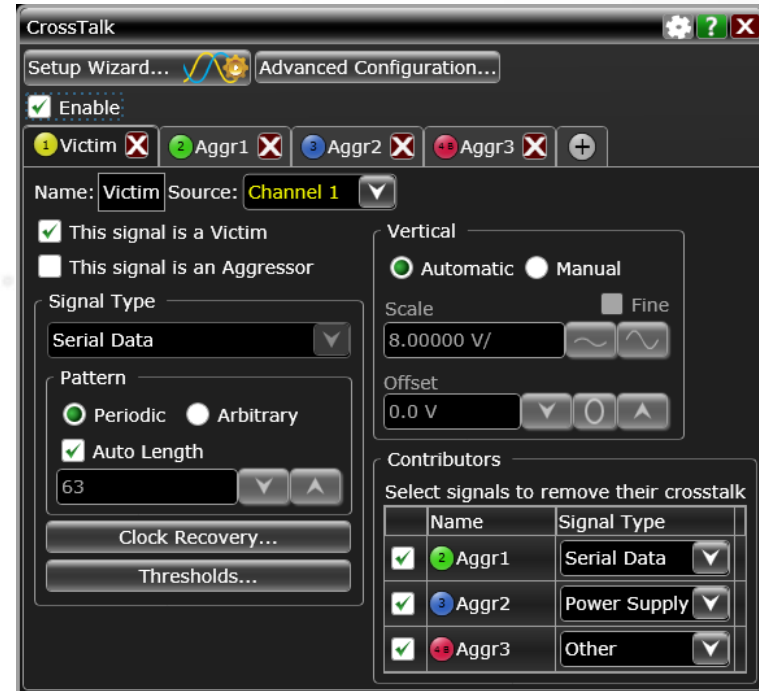
Power supply aggressor signal

Original serial data victim signal

Serial data victim signal with crosstalk removed

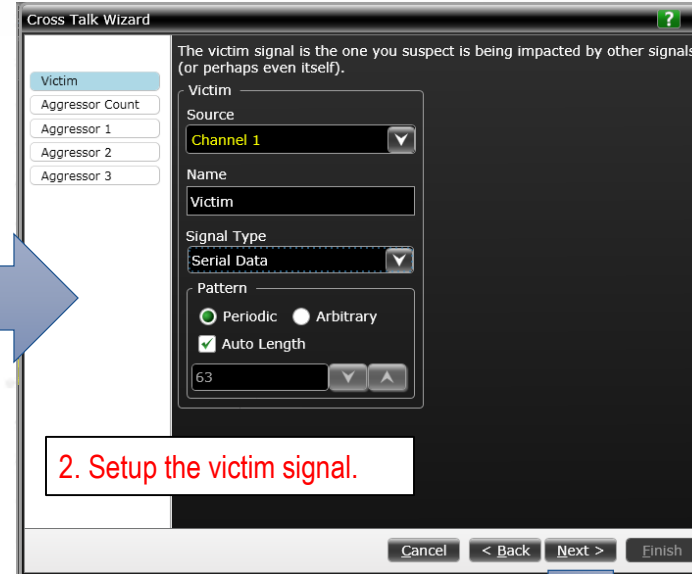
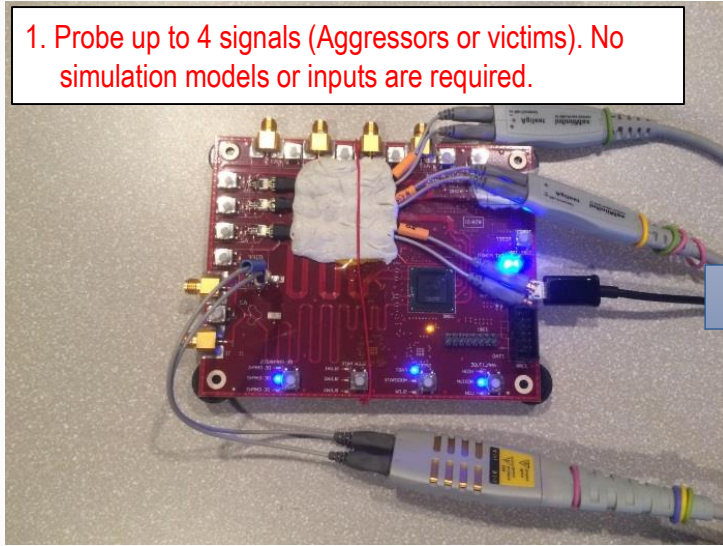
# Features of the N8833A Crosstalk Analysis Application

1. Analyze up to four signals (victim or aggressor) at once.
2. Remove Near-End Crosstalk (NEXT), Far-End Crosstalk (FEXT) and Power Supply Crosstalk from Victim signal.
3. Plot waveform without crosstalk on the scope which can be:
  - Used for eye diagram, [jitter decomposition](#), de-embedding, equalization and mask test
  - Saved as a waveform file

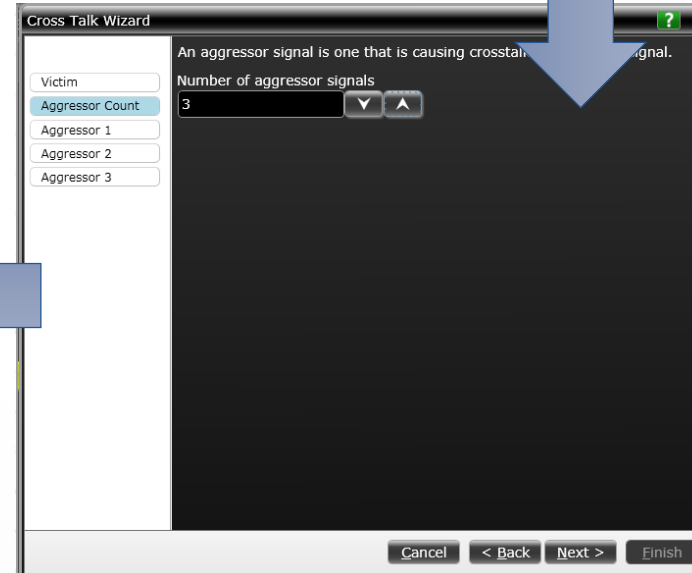
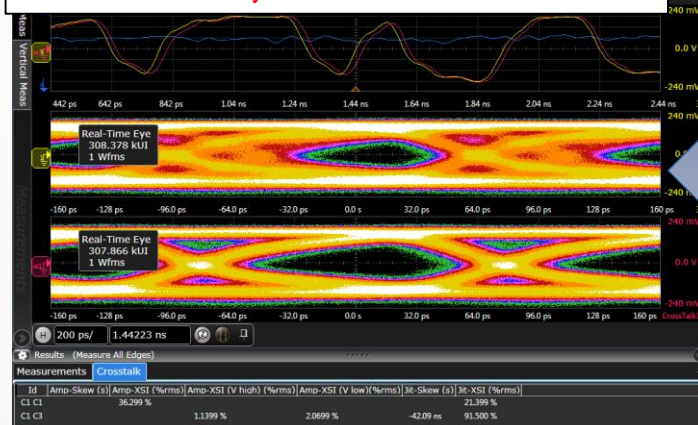


# Crosstalk Analysis Setup

1. Probe up to 4 signals (Aggressors or victims). No simulation models or inputs are required.

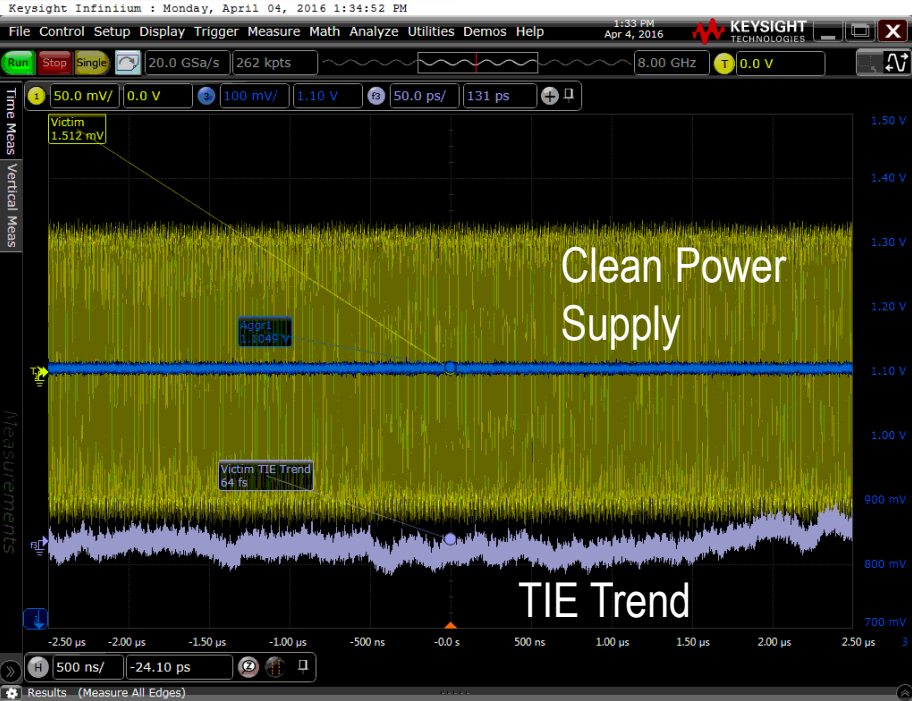


4. The app reports the amount of crosstalk from each aggressors and return a waveform without crosstalk for analysis.

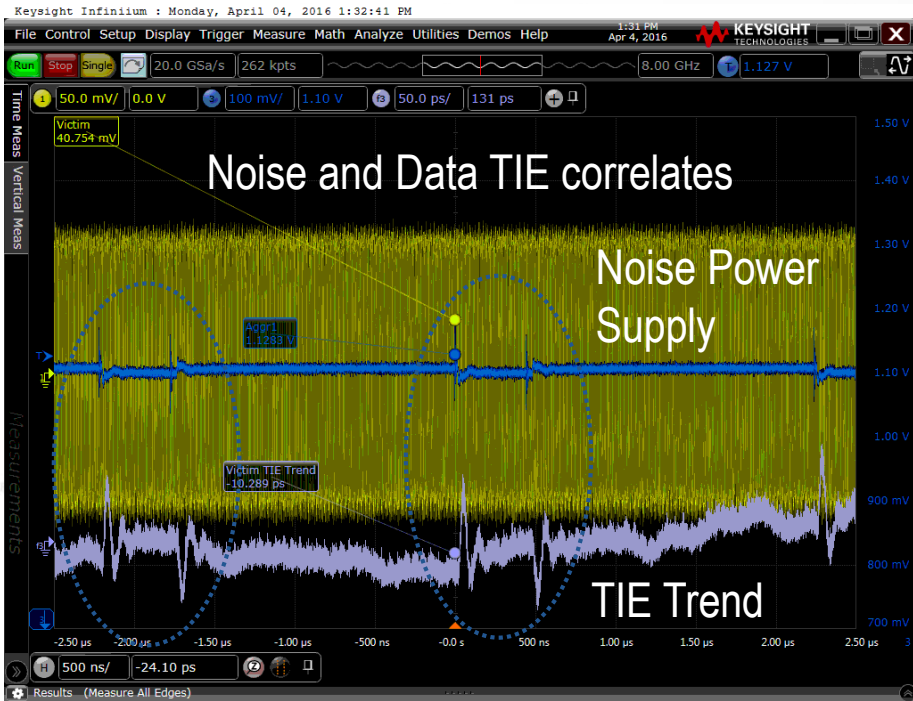


# Power Supply Crosstalk on Victim

No Power Supply Aggressor

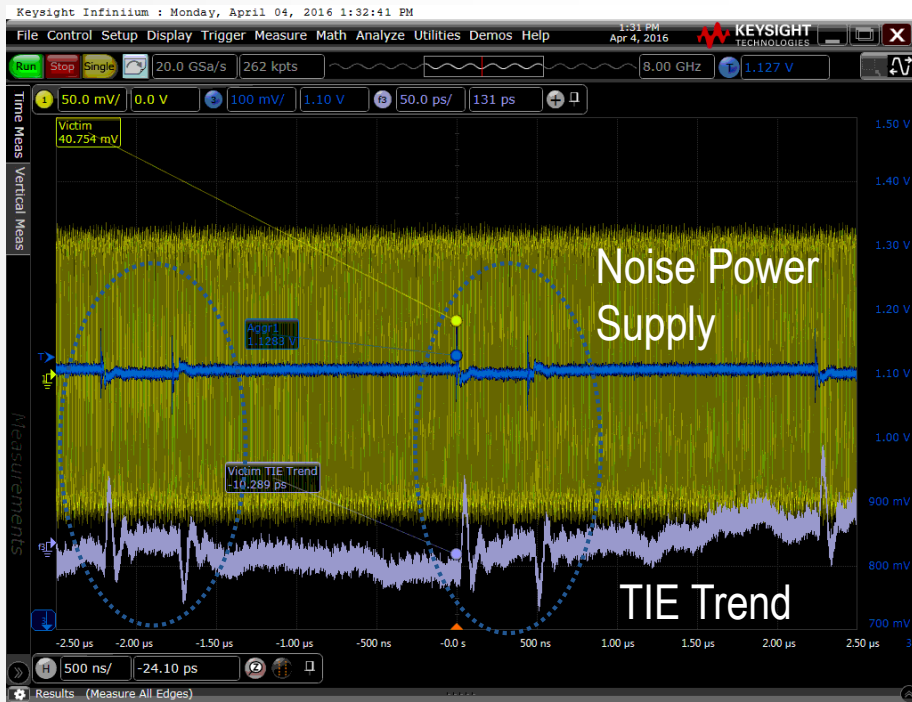


With Power Supply Aggressor on the Transmitter PLL

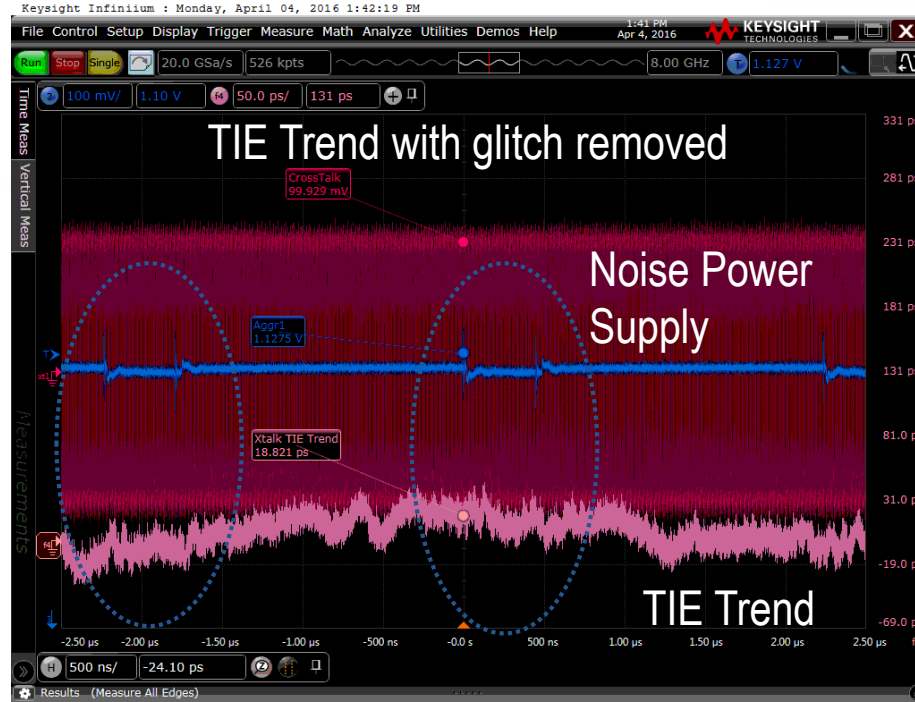


# Removing Power Supply Crosstalk from Victim

With Power Supply Crosstalk on the Transmitter PLL



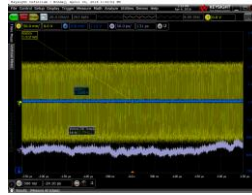
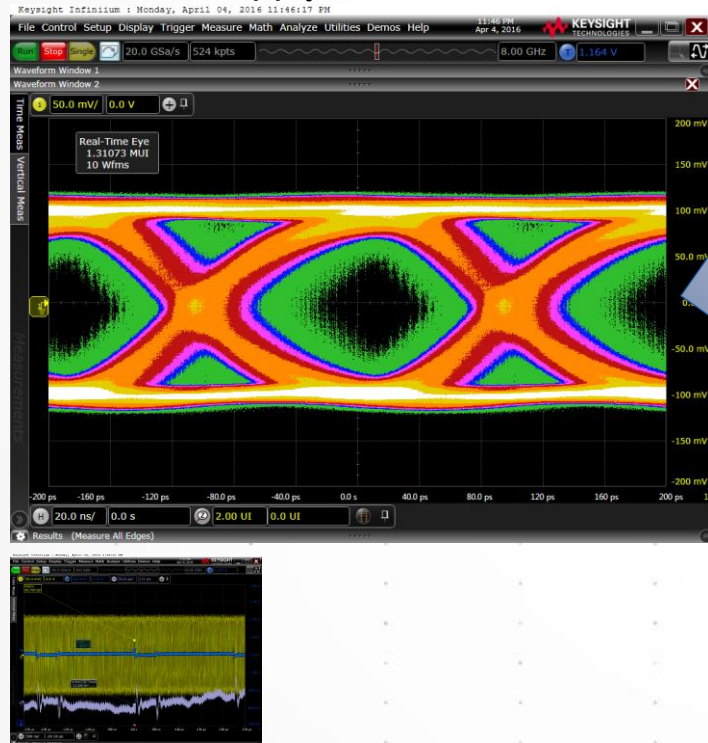
Power Supply Crosstalk Removed with Improvement on Data TIE Trend



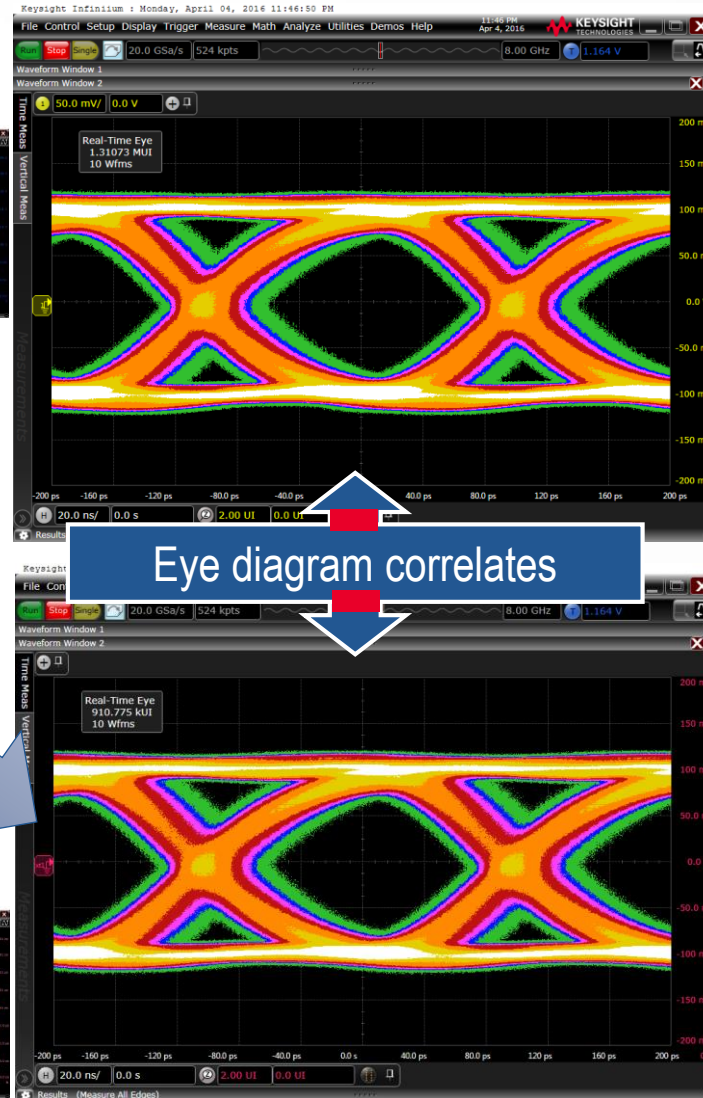


# Removing Power Supply Crosstalk from Victim

Measured Victim with Power Supply Crosstalk



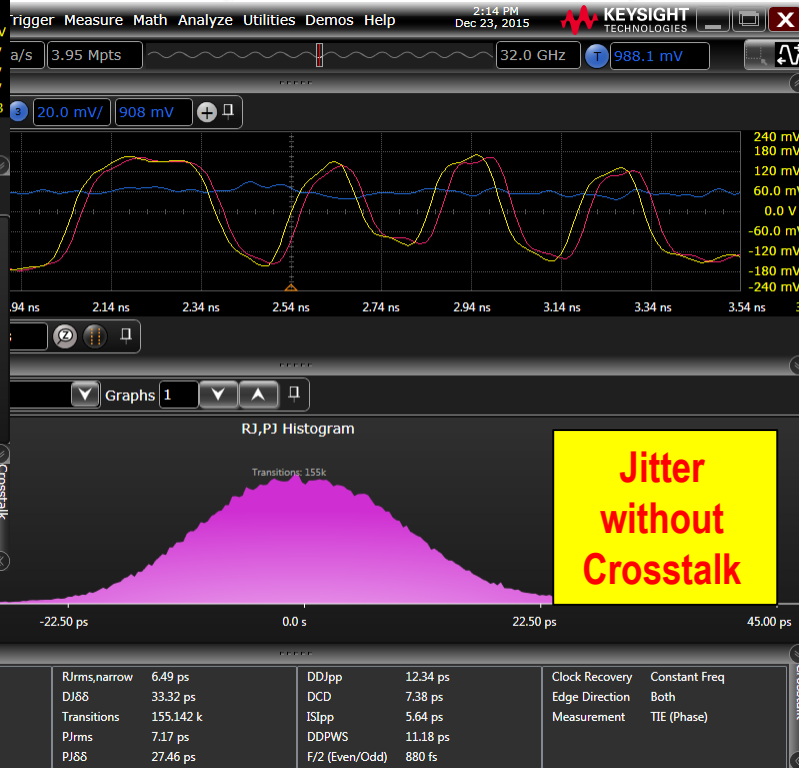
Measured Victim Without Crosstalk



Victim after Power Supply Crosstalk removed

# Jitter Improvement Without Power Supply Crosstalk

Compare jitter results before and after crosstalk removal.



TJ = 158ps

PJdd = 58ps

DJdd = 68ps

An Improvement of 20% to Total Jitter without Crosstalk.

TJ = 124ps

PJdd = 27ps

DJdd = 33ps



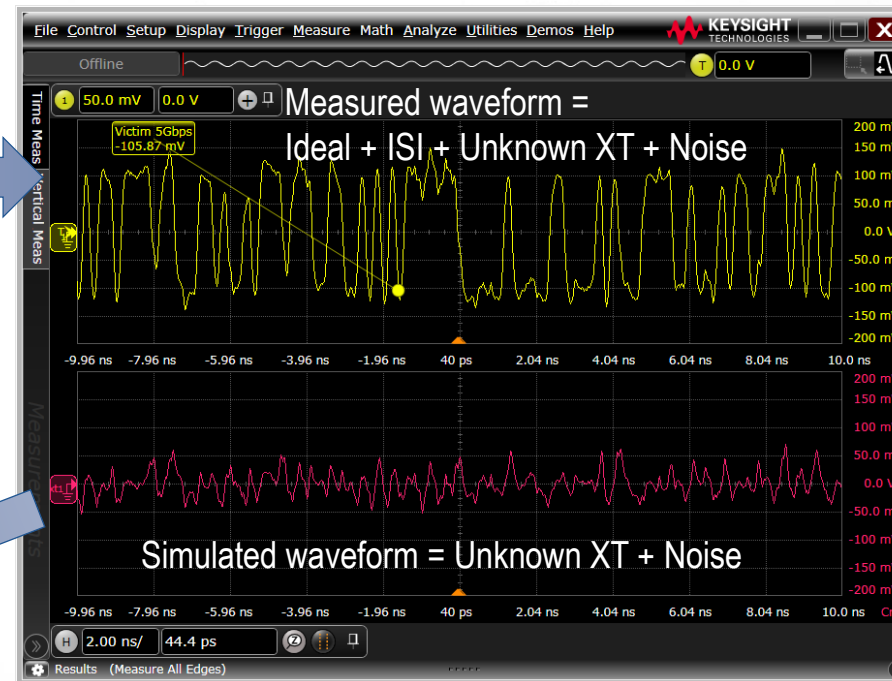
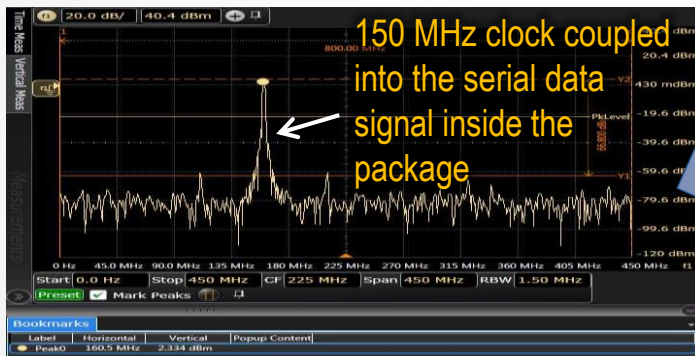
# Analyze Crosstalk & Noise that Contributes to Jitter

- The crosstalk application can remove the ideal, ISI and return “Unknown Crosstalk + Noise” (residual) content.
- Perform further analysis on this residual waveform with measurements such as FFT, markers, etc. to root cause the source of aggressor.

Remove: Ideal + ISI of Victim

Show: Only “Unknown Crosstalk + Noise”

Contributors		
Select signals to remove their contributions		
	Name	Signal Type
<input checked="" type="checkbox"/>	1 Ideal Victim Wfm	Serial Data
<input checked="" type="checkbox"/>	1 ISI of Victim	Serial Data
<input type="checkbox"/>	1 Unknown XT + Noise	Serial Data



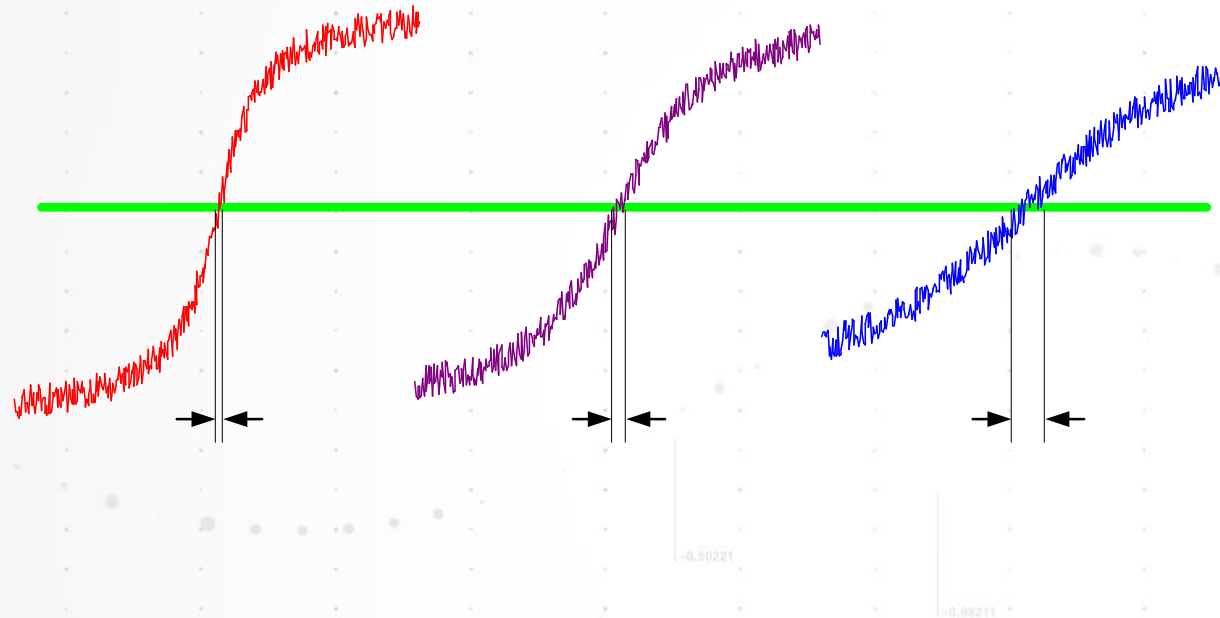
FFT on “Unknown Crosstalk + Noise”

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# Influence of Scope Noise to Jitter Performance

Random jitter will vary with slew rates.



TIE:

$$\sqrt{\left(\frac{\text{Noise}}{\text{SlewRate}}\right)^2 + \text{SampleClock Jitter}^2} \quad \text{sec rms}$$

Periodic Jitter:

$$\sqrt{2} \cdot \sqrt{\left(\frac{\text{Noise}}{\text{SlewRate}}\right)^2 + \text{SampleClock Jitter}^2} \quad \text{sec rms}$$

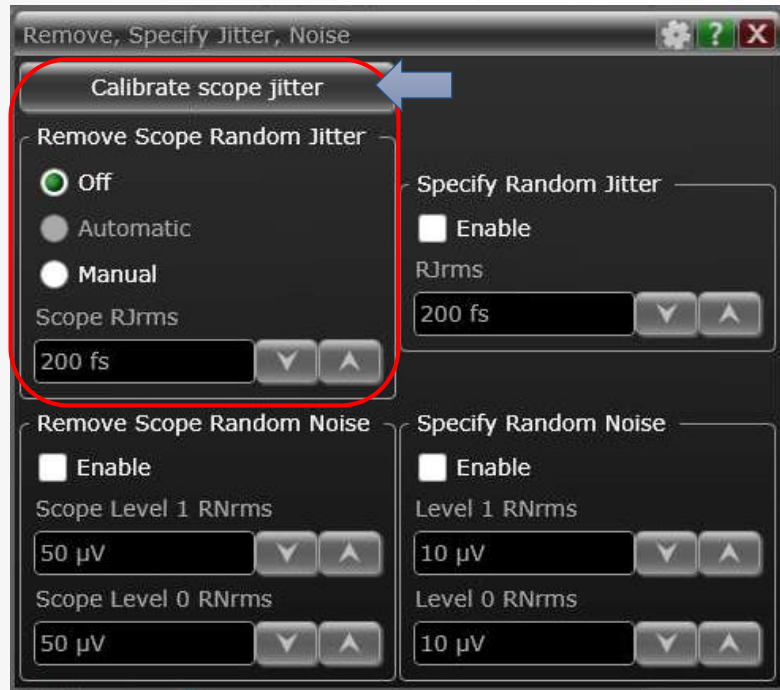
Cycle-Cycle:

$$\sqrt{3} \cdot \sqrt{\left(\frac{\text{Noise}}{\text{SlewRate}}\right)^2 + \text{SampleClock Jitter}^2} \quad \text{sec rms}$$

1. Every scope has intrinsic vertical noise floor. This vertical noise can translate into horizontal jitter.
2. As signal slew rate decreases, vertical noise increases the random jitter.
3. Measured random jitter is a function of signal slew rate, scope noise and scope sample clock jitter.

# Scope Random Jitter Removal

Calibrate and remove scope random jitter contribution



- Scope RJ calibration is available to remove the contribution of scope noise to measured RJ.
- User is asked to disconnect the signal from Channel to measure the  $ACV_{rms}$  noise for the current Vertical setting.

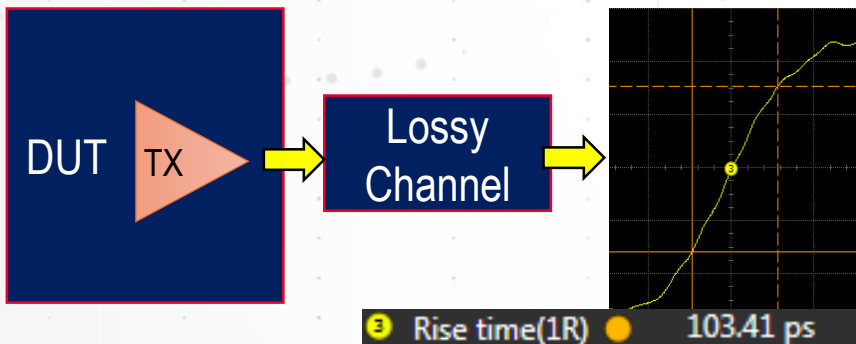
# Other Jitter Measurement Considerations

Gain Margin by removal of Scope contribution to RJ



Signal with Fast Rise Time

TJ(1E-12)	7.115 ps
RJrms,narrow	347 fs
DJ88	2.236 ps



With no Scope RJ removal

TJ(1E-12)	26.96 ps
RJrms,narrow	1.28 ps
DJ88	8.99 ps

After Scope RJ removal

TJ(1E-12)	14.43 ps
RJrms,narrow	340 fs
DJ88	9.70 ps

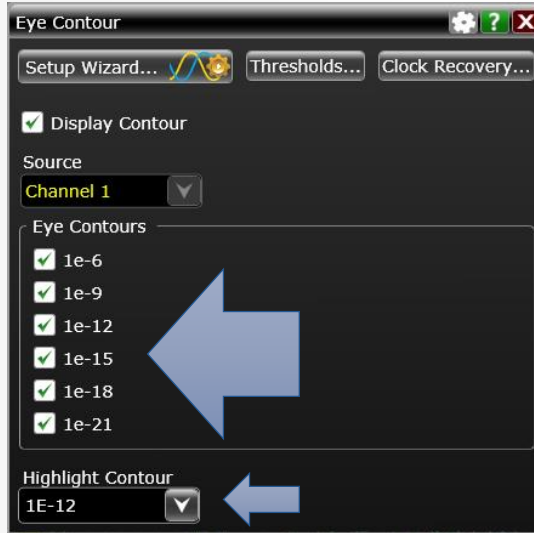
Gain margin through scope RJ removal.

# Agenda

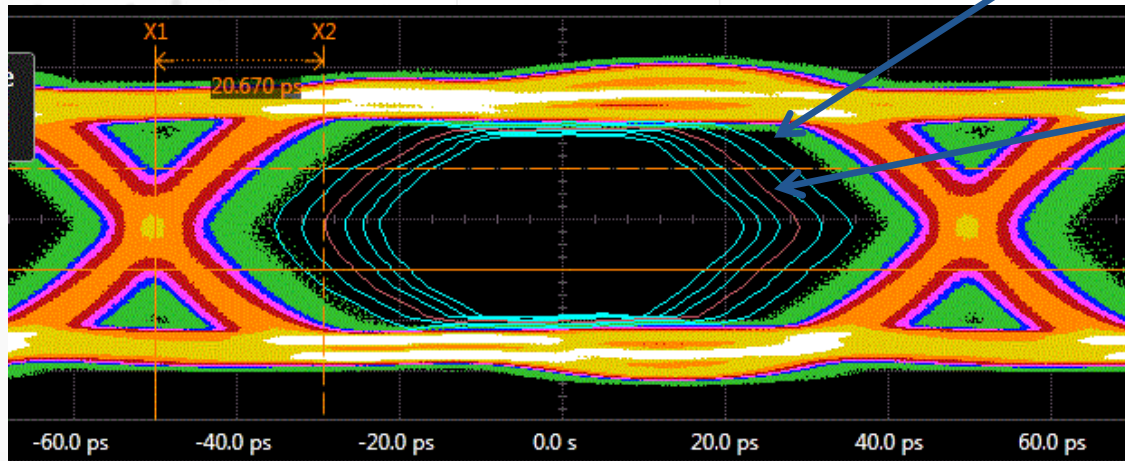
- Review of Jitter Decomposition
- Assumptions and Limitations
- Spectral vs. Tail Fit Method
- Jitter Analysis with Crosstalk Removal Tool
- Scope Random Jitter Removal from Jitter Analysis
- Other Tools to Consider for Jitter Analysis
- Summary

# Jitter Analysis with BER Eye Contour

Estimate Jitter and Eye Opening to various BER level



- Specify the BER eye contours you want the scope to plot.
- Specify which BER contour to highlight in red.



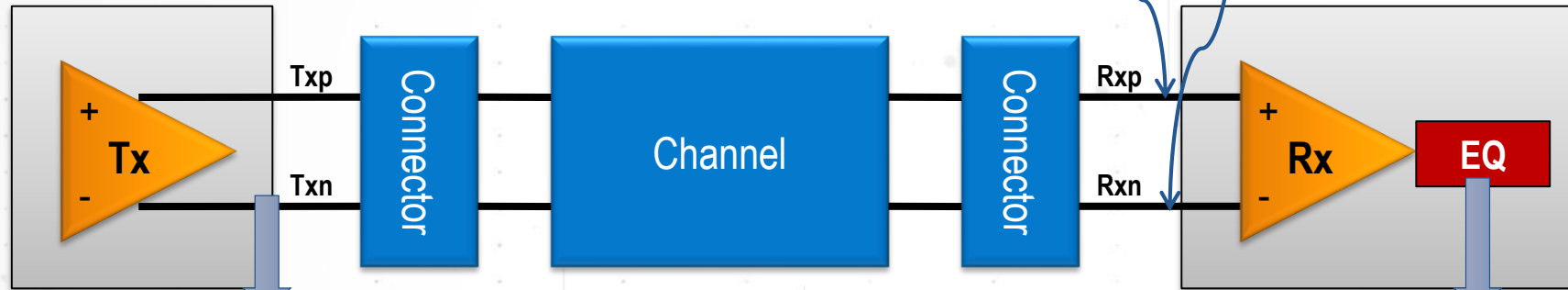
BER Eye Contours

Eye Contour at BER  $10^{-12}$



# Analyze Jitter at Various Test Points

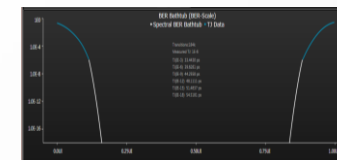
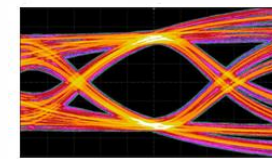
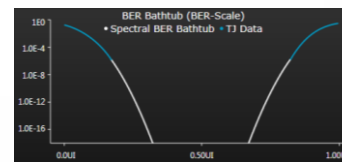
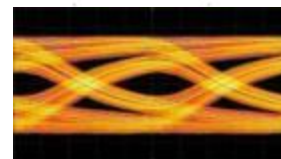
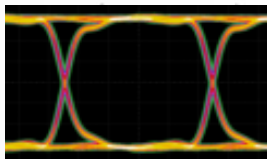
Jitter Analysis with De-embedding and Equalization



After Scope De-embedding to the TX point

Measurement Node

After Scope Equalization

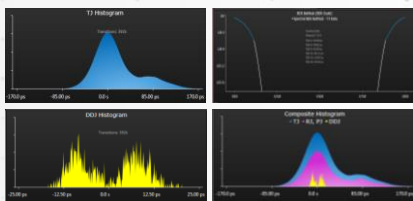




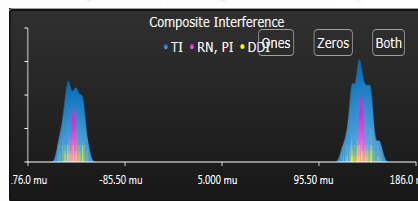
# Agenda

- Review of Jitter Decomposition
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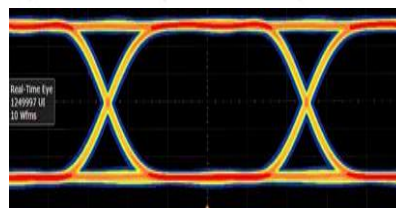
# Keysight Real-Time Scope Jitter Analysis Tools



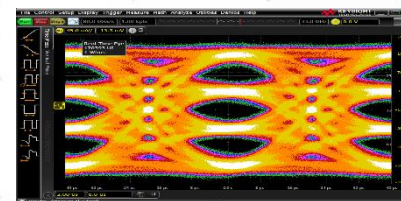
N5400A EZJIT Plus for Jitter Analysis and RJ Scope Removal Calibration



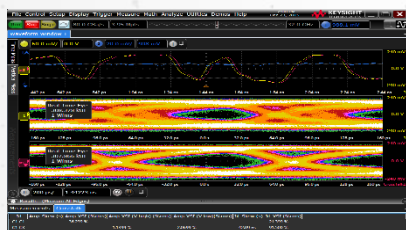
N8823A EZJIT Complete for Vertical Noise Analysis



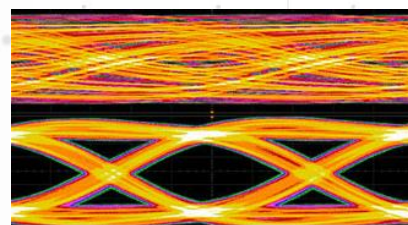
E2688A High-Speed SDA for Reference Clock Recovery and Eye Analysis



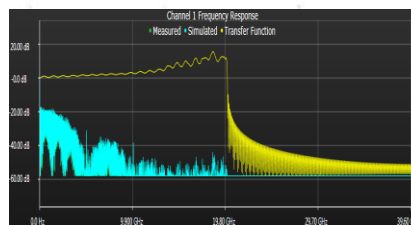
N8827A PAM-4 Clock Recovery



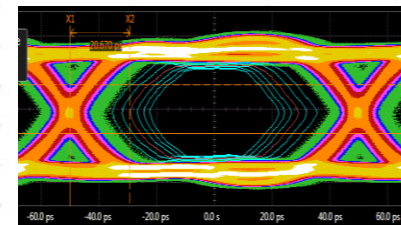
N8833A Crosstalk Analysis and Removal Application



N5461A Serial Data Equalization Software

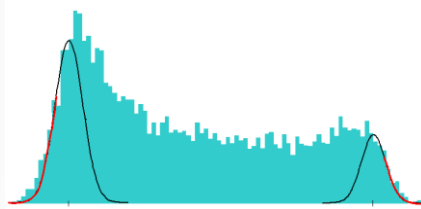


N5465A InfiniiSim De-embedding Software

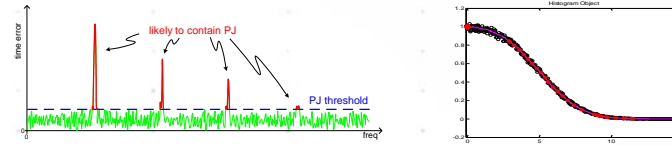


BER Eye Contour Comes standard with E2688A and N8823A

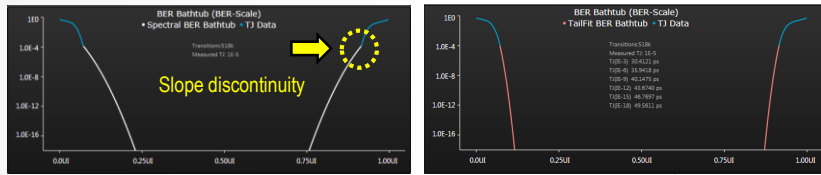
# Jitter Analysis Summary



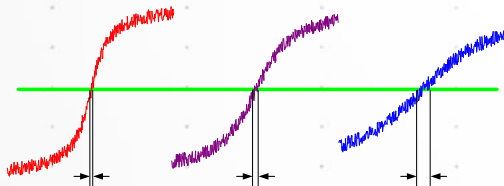
Dual Dirac Model for Jitter Decomposition



Spectral vs. Tail Fit for ABUJ (Crosstalk) Jitter Analysis



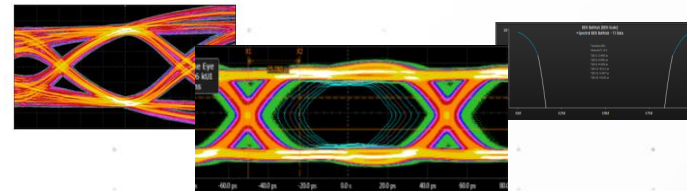
Use Smoothness of Slope Continuity on the Bathtub Curve



Scope Random Jitter Removal



Use Crosstalk Removal Tool to Recover Jitter Margins



BER Eye Contour, De-embedding and Equalization for Jitter Analysis